SYNTHESIS AND MAGNETIC PROPERTIES
OF Sn, Mn AND Mg SUBSTITUTED Fe$_x$Cr$_{1.8-x}$O$_3$
NANO OXIDES

by

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Abstract

The synthesis, structure characterization and magnetic properties of a series of (Sn, Mn, Mg)$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nano oxides have been studied. These alloys series were synthesized at low reaction temperature of about 100 $^\circ$C using hydrothermal methods. Single-phase hexagonal corundum structure and nanoparticle structure of the synthesized samples were confirmed by X-ray diffraction (XRD) and transmission electron microscopy (TEM). The refinement of XRD data was performed by Rietveld analysis using a model involving a combination of both interstitial and substitutional Mg$^{2+}$, Mn$^{2+}$, and Sn$^{4+}$ ions in octahedral coordination. The structural and magnetic properties of Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples prepared using two different methods are compared. XRD analysis for the samples synthesized in a stirred pressure reactor and in a reflux indicate the basic corundum structure for the compositions. TEM experiment indicate a similar trend for both methods of preparation with a particle size for samples prepared in a pressure reactor slightly reduced compared to that synthesized in a reflux. No appreciable difference was observed on the magnetic properties of the two sets of samples. Particle sizes and chemical disorder are shown to play critical roles in influencing the properties of (Sn, Mn, Mg)$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nanomaterials. The $^{57}$Fe Mössbauer spectra measured at room temperature are well fitted by two magnetic components that range from two sextets for Fe-rich nanomaterials to two doublets for Cr-rich ones. Increased Cr substitution is associated with increased negative exchange interactions. The analysis of the Mössbauer spectra show evidence of Fe$^{3+}$ ions at lattice sites with and without Cr, Sn, Mn or Mg ion neighbors. The transition from sextets to doublets can also be attributed to increased chemical disorder of Fe$^{3+}$ ions with increase in Cr content. The variation of coercive field with particles size reveals that the coercive field achieves a maximum at a critical particle size. These results show evidence of transformation from multi- to single-domain structures. The investigation of the structure
and magnetic properties of $\text{Mg}_0.2\text{Fe}_{x}\text{Cr}_{1.8-x}\text{O}_3$ nano oxides confirmed the corundum structure in the alloys system. The interpretation of ZFC and FC magnetization results suggest evidence of spin freezing and this behavior at low temperature appears to be associated with increased magnetic hardness. The magnetic susceptibility at high temperature follow the Curie-Weiss relationship with large negative values of Weiss temperature constant, $\theta_p = -354$ K and -722 K. These large negative values of $\theta_p$ are interpreted as a robustness of the antiferromagnetic interactions in this alloy system. The effect of annealing temperature on the exchange bias in $\text{Mg}_0.2\text{Fe}_{x}\text{Cr}_{1.8-x}\text{O}_3$ was also investigated. The shift of the hysteresis curve along the field axis observed in the magnetization results are interpreted as the exchange bias effect. There is a strong correlation between the exchange bias field $H_{EB}$ and the particle sizes $D$ which leads to a critical particle size at about 33 nm. Finally the results on the structure and magnetic properties of $\text{Mn}_0.2\text{Fe}_{x}\text{Cr}_{1.8-x}\text{O}_3$ nano oxides suggest that this alloy system is superparamagnetic at room temperature. The exchange bias effect is found to be different to that observed in the $\text{Mg}_0.2\text{Fe}_{x}\text{Cr}_{1.8-x}\text{O}_3$ alloys. The magnetic susceptibility results follow the Curie-Weiss relationship with a negative Weiss temperature constant $\theta_p = -175$ K, which is relatively small compared to that obtained for the $\text{Mg}_0.2\text{Fe}_{x}\text{Cr}_{1.8-x}\text{O}_3$ alloys. The small value is interpreted as a weaker antiferromagnetic interaction in the material.
Preface

The experimental work described in this dissertation was carried out in the Condensed Matter Physics Laboratory, School of Chemistry and Physics, Westville Campus, University of KwaZulu-Natal, Durban under the supervision of Dr. Thomas Moyo.

The study represents original work by the author and have not otherwise been submitted in any form for any degree or diploma to any tertiary institution. Where use has been made of the work of others it is duly acknowledged in the text.
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1. Effects of annealing on exchange bias in Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ compounds prepared via the hydrothermal route, K. Mbela, T. Moyo, S.E Nadir Osman, Journal of Materials Science: Materials in Electronics DOI 10.1007/s10854-016-4919-1 (2016) (Published online 3 May 2016).


Dedication

Now unto him that is able to do exceedingly abundantly
above all that we ask or think,
According to the power that worketh in us,
For in him we live, and move, and have our being; ...
Unto him be glory...
By Christ Jesus throughout all ages.

Amen.

Eph 3:20, Act 17:28
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Chapter 1

Introduction

1.1 Defining the nanoscale

Nanoscale materials are defined as substances in which at least one dimension is less than approximately 100 nm. A nanometer is one millionth of a millimeter and that is approximately $10^5$ times smaller than the diameter of a human hair [1]. Nanomaterials are interesting because at this scale unique optical, magnetic, electrical and other properties emerge. These novel properties often originate from the high surface area to volume ratio in structures of this size. Surface effects, which are often negligible when studying bulk materials become significant. These emergent properties that are different for materials of the same chemical composition in their nano and bulk forms have the potential for significant impacts in several fields such as electronics, medicine, biotechnology, biomedical, material science, engineering, and environmental areas [2–5]. Nanoparticles have nanoscale dimensions in every direction. A variety of methods are used to prepare nanoparticles which include chemical vapor deposition [6], sputtering [7], microemulsion polymerization [8], mechanical milling [9, 10] and wet chemistry methods [11]. For size-dependent physical properties, highly monodispersed samples are desirable [12]. Several different classes of nanoparticles can be produced. Some of the most extensively studied magnetic nanoparticles are metals, nanoparticle of rare earth metals, magnetic alloys, ferrites and magnetic oxides [13, 14]. However
in this work we consider structural and magnetic properties of doped \( \text{Cr}_2\text{O}_3 \) or \( \text{Fe}_2\text{O}_3 \) nanoparticle oxides.

### 1.2 Brief overview of iron oxides

The term “iron oxide” can also be used as a generic name for iron hydroxides, oxyhydroxides and other related compounds and have been known for millenia [15]. Such minerals were used originally as pigments for paints during the Palaeolithic. Much later, the materials were used in magnetic compasses when they were discovered in China. This was in fact the first application of magnetic iron oxides, also known as lodestones, used by early navigators to locate the magnetic North. Iron oxides have received increasing attention due to their extensive applications such as magnetic recording media, catalysts, pigments, gas sensors, optical devices, and electromagnetic devices [16]. The oxides exist in a rich variety of structures (polymorphs) and hydration states. Among several crystalline modifications of anhydrous ferric oxides there are two common magnetic phases, namely, rhombohedral hematite (\( \alpha\text{-Fe}_2\text{O}_3 \)) and cubic maghemite (\( \gamma\text{-Fe}_2\text{O}_3 \)). In the \( \alpha\)-phase, all \( \text{Fe}^{3+} \) ions have an octahedral coordination, whereas in \( \gamma\)-phase having the structure of a cation-deficient \( AB_2\text{O}_4 \) spinel, the metal atoms \( A \) and \( B \) occur in tetrahedral and octahedral environments, respectively. The oxide \( \alpha\text{-Fe}_2\text{O}_3 \) is antiferromagnetic at temperatures below 950 K [17], while above the Morin point (260 K) [18] it exhibits weak ferromagnetism. Hematite, the thermodynamically stable crystallographic phase of iron oxide with a band gap of 2.2 eV is a very attractive material because of its wide applications especially in catalysis, gas sensors, pigments, and paints [19]. Its nontoxicity is an attractive feature in these applications.

In the present work, the study of mixed metal oxides has been undertaken in order to investigate the evolution of properties as a function of synthesis method, composition and temperature of the samples [16]. \( (\text{Sn, Mn, Mg})_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3 \) are examples of
mixed oxides which we have produced and studied [20, 21]. These oxides have been produced by low temperature synthesis using a reflux method and a stirred pressure reactor. High-energy ball milling has been used to reduce the particle sizes. The nano oxides produced reveal interesting properties which are the subject of this thesis.

1.3 Crystal structure

Several iron oxides share the same crystal structure with other minerals. For instance, goethite is isostructural with diaspore (α-AlOOH), magnetite with spinel (MgAl$_2$O$_4$) and hematite with corundum (Al$_2$O$_3$) [22]. Thus, the denomination corundum oxides for the later case. The structure of pure corundum consists of octahedral sites within a trigonal crystal system in which metal cations fill two thirds of the octahedral sites and oxygen anions are present in one third of the octahedral sites. Each oxygen is shared between 4 octahedra. The unit cell parameters are as follows; $a = b = 4.75$ Å, $c = 12.982$ Å, $\alpha = \beta = 90^\circ$, $\gamma = 120^\circ$. Figure 1.1 shows a sketch of a corundum structure [23].

![Crystal structure of corundum](image)

**Figure 1.1**: Crystal structure of corundum (metal gray, Oxygen black).
1.3.1 The octahedral site

In pure corundum structure six oxygen atoms surround each aluminium atom in the form of a slightly irregular octahedron due to the non-existent centre of symmetry. The three oxygen atoms above the metal atom are closer to each other than the three oxygen atoms below. Due to the large ratio of the radius of the oxygen (1.40 Å) anion to the radius (0.57 Å) of the metal cation, the metal cations are located between the closely packed oxygen anions as shown in Figure 1.2 [23].

Figure 1.2: Crystal structure of Alumina (corundum). The octahedral sites are visible.
1.3.2 Cations distribution

Figure 1.3 shows the distribution of cations in the crystal structure of alumina (corundum). In terms of the ionic bonding, the positively charged metal ion is surrounded by six negatively charged oxygen ions. Each metal atom gives up three electrons to become a metal ion of valency $3^+$ and does not have any unoccupied energy levels. Similarly, the oxygen atom receives two electrons to become an oxygen ion of valency $2^-$ and does not have any unoccupied energy levels [24]. This produces an electrostatic field around the metal cations, also known as a crystal field. The crystal fields within the corundum allow metal impurities to bind to the crystal because the chemical bonding between the corundum and the guest impurity will always involve the donation of electrons from the corundum to the metal impurity. For example, impurities such as titanium and iron will change the form of the corundum to a colored sapphire. A chromium impurity will transform the colorless corundum crystal into a red ruby. In pure corundum all the electrons in the crystal are paired. This disables the ability of the crystal to absorb any light and hence the absence of colour in pure corundum results [24].

Figure 1.3: (a) Corundum structure in $\alpha$-$\text{Al}_2\text{O}_3$, (b) top view of the corundum structure, and (c) octahedral structure of $\alpha$-$\text{Al}_2\text{O}_3$. 
1.4 Synthesis of metal oxides

The synthesis of single and mixed metal oxides by simple low cost methods and in high yield has been a challenge since the early development of Nanoscience. Various approaches have been developed so far for the commercial production of metal oxides. The oxides in the bulk and nanosize forms can be produced by solid state reaction and wet chemistry methods [25, 26]. Solid state reaction has been used intensely to produce mixed metal oxides in the bulk form. The starting materials in this technique are usually high purity metal oxides. This method involves prolonged double sintering at high temperatures of at least 1000 °C and as high as 1400 °C. The elevated temperatures might cause some of the constituent materials to evaporate thus unbalancing the stoichiometry. Mixed metal oxides materials can also be made by high-energy ball milling where the mechanosynthesis of the nanostructures is promoted by the mechanical activation of the chemical reactions involved in the formation of the oxides. The oxide mixtures are milled for several hours in agate or hardened steel jars with an appropriate number of balls. Good quality samples and the desired phase form if the milling conditions such as grinding ball to sample mass ratio, the rotation speed of the jars and the atmosphere in the jars are well defined. Although nanoparticles can be directly produced by this method, as is the case for grinding in the conventional ceramic method, some sample is lost by sticking to the hardened steel jars and balls which may affect the stochiometric composition. During the grinding process undesired impurities from the grinding surface may also contaminate the sample. When milling in oxygen atmosphere, possible changes in stoichiometry of the sample can also occur due to the formation of metal oxides. Mixed metal oxides can also be synthesized by the combustion process where metal nitrates are mixed with a fuel such as urea and then heated up to generate an exothermic reaction after self-ignition of the mixture [9]. Co-precipitation methods are simple methods of synthesizing nanoparticles from
salts such as nitrates, chlorides, sulfates and perchlorates. With the appropriate ratios of the precursor salts, it is possible to obtain a narrow size distribution of spherical nanoparticles \([25, 27, 28]\). As an alternative method, the polyol process, uses polyols such as ethylene glycol. Polyols are boiling solvents, reducing agents and stabilizers that control the growth and prevent the aggregation of nanoparticles. This method is useful for the preparation of dispersed nanoparticles with tailored sizes and tuneable properties \([28]\). Thermal decomposition at appropriate conditions will yield monodispersed nanocrystals in one reaction without a further size-selection process. Large scale amounts of material can be produced because inexpensive reagents can be used \([26]\). The samples studied here were produced by hydrothermal method which involves aqueous solutions at atmospheric or higher vapor pressures. This technique is very effective in controlling the size and shape of nanocrystals. The starting materials are high-purity metal chlorides or nitrates mixed with a precipitating reagent such as \(\text{NH}_3\), \(\text{NaOH}\) or \(\text{KOH}\). The technique has the advantage of eliminating impurities compared to the synthesis by solid state reaction. A detailed discussion of the technique and equipment used is given in chapter 4.

1.5 Magnetic properties

There are various forms of magnetism that arise in solids depending on how the constituent magnetic moments interact with each other. The magnetic properties are determined by the magnetic interactions between magnetic moments which depend on the location of metal cations in the crystal structure \([29]\). Bulk antiferromagnets are magnetically inactive materials due to the antiparallel arrangement of spins. Antiferromagnetic (AF) order in metal oxides, such as hematite \((\alpha-\text{Fe}_2\text{O}_3)\), results from the superexchange interaction between the \(\text{Fe}^{3+}\) spins mediated by neighboring oxygen ions. A considerable fraction of the spins on the surface are uncompensated. However,
their contribution is insignificant in bulk materials. Bulk hematite present the Morin transition \( (T_M \approx 260 \text{ K}) \), which is the magnetic change from a high-temperature weakly ferromagnetic phase to a low-temperature antiferromagnetic phase caused by spin canting. The crystal structure of hematite is similar to that of corundum \((\text{Al}_2\text{O}_3)\) and it can be described as a rhombohedral structure with R-3c space group. Moreover, it has been reported that the Morin transition depends on crystallite size, impurities, strain and defects [30–32]. In Figure 1.4 we show the Mössbauer spectrum of a bulk iron (III) oxide powder with particle size \(< 5 \ \mu\text{m}\) and purity \(\geq 99\%\) (SIGMA-ALDRICH) (measured at room temperature in the Condensed Physics Laboratory (UKZN). In nanostructured magnetic materials, mixed metal interactions between nanoparticles play an important role. Long-range magnetic interactions can have a strong influence on the magnetic dynamics in a sample containing ferromagnetic or ferrimagnetic nanoparticles [33]. If nanoparticles are in close proximity, exchange interactions between surface atoms can be significant. An important example of magnetic proximity effects is exchange bias, which manifests itself as a shift in the hysteresis loop below the Curie temperature [34]. The magnetic properties of weakly interacting magnetic nanoparticles are strongly in-

Figure 1.4: Room temperature Mössbauer spectrum of the bulk hematite \((\alpha-\text{Fe}_2\text{O}_3)\) powder.
fluenced by superparamagnetic relaxation at finite temperatures. Mössbauer studies of hematite (α-Fe₂O₃) [30–32] nanoparticles have shown that the superparamagnetic relaxation of antiferromagnetic nanoparticles can be significantly suppressed if the particles are in close proximity. This has been explained by exchange interaction between surface atoms of neighboring particles [30, 35]. André-Filho et al. [36] have studied the size dependence of the magnetic and hyperfine properties of nanostructured hematite (α-Fe₂O₃) powders prepared by the ball milling technique. They obtained well-resolved magnetic sextets at room temperature as shown in Figure 1.5. This implies that the thermal relaxation effects associated with the nanostructured samples are not present. Due to the asymmetric shape and the peaks broadening with the milling time, the fits of the spectra were carried out using a histogram distribution of sextets for the milled samples. In Table 1 are listed the hyperfine parameters, the distribution width and spectral areas determined from the fits. In all samples, the inclusion of a sextet consistent with the presence of α-Fe is in agreement with the structural analysis [36].

![Figure 1.5: Room temperature Mössbauer spectra of the milled hematite powders.](image)
### Table 1.1: Hyperfine parameters from Mössbauer spectra recorded at room temperature for the Bulk hematite and milled powders.

<table>
<thead>
<tr>
<th></th>
<th>Hematite</th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>δ mm/s</td>
<td>Δ mm/s</td>
<td>$B_{hf}$ kOe</td>
<td>W (T) %</td>
<td>α-Fe f %</td>
</tr>
<tr>
<td>Bulk</td>
<td>± 0.01</td>
<td>± 0.01</td>
<td>± 0.1</td>
<td></td>
<td>[Figure 1.4]</td>
</tr>
<tr>
<td>Milled (1 h)</td>
<td>0.36</td>
<td>-0.12</td>
<td>515.6</td>
<td>100</td>
<td>4 [34]</td>
</tr>
<tr>
<td>Milled (5 h)</td>
<td>0.35</td>
<td>-0.18</td>
<td>493.2</td>
<td>2.5</td>
<td>96</td>
</tr>
<tr>
<td>Milled (10 h)</td>
<td>0.36</td>
<td>-0.16</td>
<td>486.4</td>
<td>2.9</td>
<td>93</td>
</tr>
</tbody>
</table>

### 1.6 Some applications of iron based oxides

Iron based oxides nanoparticles show a wide variety of anomalous magnetic properties compared to their respective bulk materials. The magnetic properties of small particles are strongly influenced by finite-size effects [37]. The relevance of these effects increases with decreasing particle size. Finite size effects result from the quantum confinement of the electrons, whereas typical surface effects are related to the symmetry breaking of the crystal structure at the boundary of each particle [38]. Small magnetic particles exhibit unique phenomena such as superparamagnetism, quantum tunnelling and unusually large coercivities. Iron oxides can also be used as colouring and coating materials. The use of hematite and other iron oxides as natural red ceramic pigments has been practiced since prehistoric times. Iron oxides such as magnetite, hematite, maghemite and goethite are commonly used as pigments for black, red, brown and yellow colours respectively. Predominantly natural red iron oxides are used in primers for steel construction and reduction of corrosion problems in cars [39]. Iron oxide-based materials have been found to be good candidates for cheap and efficient...
catalysts. Magnetite and hematite are widely used to enhance oxidation/reduction and acid/base reactions. The catalytic activities of Fe$_2$O$_3$ has been reported by Sohn and Jim [40]. Multi-walled carbon nanotubes have been synthesized using Cr$_{2-x}$Fe$_x$O$_3$ solid solutions as catalysts [41]. Iron and titanium mixed oxides have been found to be catalytically active for the reactions of cyclohexane oxidation [42], $\alpha$-pinene oxide isomerization, O-Cresol photo-degradation [15] and formation of dimethyl ether from methanol. Fe$_2$O$_3$ based nanomaterials have also been developed for selective catalytic reduction (SCR) of NO$_x$ by NH$_3$ in diesel exhausts [43]. A number of studies have also focused on iron oxide Fe$_2$O$_3$ which in the gamma and cubic phases exhibits good sensing characteristics towards hydrocarbon gases, carbon monoxide and alcohols [38], [39, 44, 45]. The sensitivity of iron oxide-based sensors can be enhanced further by various doping schemes. A number of different dopants such as Pd, Sn, Ti and Zn have been used [46–48]. While doping is an important factor for controlling the sensing characteristics, the sensor structure and the thickness of its active layer play a significant role on its sensitivity. Iron oxide nanoparticles are also interesting due to their wide range of applications in fields such as magnetic storage, medicine, chemical industries and water purification.

### 1.7 Motivation for current work

Ferric oxide (α-Fe$_2$O$_3$), chromic oxide (α-Cr$_2$O$_3$) and their mixed compounds have application in many fields. They can be used as catalysts for high temperature water-gas shift reaction [49] and reduction of NO$_x$ by NH$_3$ [50], as refractory materials [51] and sensing materials [52]. Their crystal structure is the same as that of corundum (Al$_2$O$_3$). α-Fe$_2$O$_3$ and α-Cr$_2$O$_3$ have different semiconducting and sensing properties. Their magnetic and structural properties are influenced by particle sizes [16, 19], degree of crystallinity [53], pressure [54] and doping [48, 55]. The effect of metal doping by tita-
nium [56, 57], tin [58, 59], manganese [60], aluminium [61, 62], gallium [63] and indium [64] on the electrical, magnetic and other physical properties of $\alpha$-Fe$_2$O$_3$ (hematite) has been investigated for some time. It is generally proposed that the dopant metal ions substitute for Fe$^{3+}$ in the corundum-related structure of $\alpha$-Fe$_2$O$_3$ with the consequent formation of cationic and anionic vacancies. The difference in ionic radius between the dopant metal ion and that for Fe$^{3+}$ will influence the structural characteristics and phase behavior of the doped system. The tin-doped $\alpha$-Fe$_2$O$_3$ system has attracted interest because of its sensing properties for gases such as methane and carbon monoxide [46, 65, 66]. The microstructure of tin-doped $\alpha$-Fe$_2$O$_3$, prepared by mechanical milling was examined by Jiang et al. [67] using Rietveld structure refinement of X-ray powder diffraction data and the results were interpreted in terms of the Sn$^{4+}$ ions occupying interstitial octahedral sites in the $\alpha$-Fe$_2$O$_3$ lattice. The properties of $\alpha$-Cr$_2$O$_3$ can also be drastically changed by varying their size and introducing dopants [68–70]. Literature suggests that introducing dopants into the sensor material is an effective way to improve sensitivity and selectivity [71]. Formation of mixed oxides leads to the modification of the electronic structure of the system. Surface properties are expected to be influenced by new boundaries between grains of different chemical composition. It is anticipated that all these phenomena will contribute advantageously to the gas sensing mechanism [71]. Undoped and doped $\alpha$-Cr$_2$O$_3$ gas sensors have been investigated for detection of toxic and combustible organic vapour. Ammonia sensing properties of Ti$^{4+}$ doped $\alpha$-Cr$_2$O$_3$ were first reported by Moseley and Williams [72]. Pokhrel et al. [73] prepared fine powders of Cr$_{2-x}$Ti$_x$O$_3$ and observed that these materials are excellent candidates for acetone monitoring. However, literature on gas sensors based on tin-chromium mixed oxides is rarely available [73], [74]. The substitution of Cr$^{3+}$ by Fe$^{3+}$ to form solid solutions of the type $\alpha$-Fe$_{2-x}$Cr$_x$O$_3$ has been known for some time [39]. Although there have been several studies of the $\alpha$-Fe$_{2-x}$Cr$_x$O$_3$ [39, 75, 76] system, there appears to have been little activity in the doping of these materials by tin. Berry
et al. [77] initiated a study of tin-doped oxides of the type $\alpha$-Cr$_2$O$_3$ and $\alpha$-(FeCr)$_2$O$_3$ and reported on their structural properties. Any systematic study of these compounds would be important. We have therefore initiated a study of these compounds to investigate how single phase formation is influenced by various factors such as the synthesis method, conditions and route. We aim to find the best substitutions to improve the properties of the iron oxides. The characteristics of the dopants are presented in Table 1.2 [78]. Therefore, we have extended our studies to include substitutions by Sn, Mg and Mn.

Table 1.2: Characteristics of the dopants.

<table>
<thead>
<tr>
<th>Dopant</th>
<th>Electronic configuration</th>
<th>Atomic radius (pm)</th>
<th>Valence</th>
<th>Possible ions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mg</td>
<td>[Ne]3s$^2$</td>
<td>145</td>
<td>2</td>
<td>Mg$^{2+}$</td>
</tr>
<tr>
<td>Mn</td>
<td>[Ar]4s$^2$3d$^5$</td>
<td>161</td>
<td>7</td>
<td>Mn$^{2+}$, Mn$^{4+}$, Mn$^{7+}$</td>
</tr>
<tr>
<td>Sn</td>
<td>[Kr]5s$^2$4d$^{10}$5p$^2$</td>
<td>145</td>
<td>4</td>
<td>Sn$^{2+}$, Sn$^{4+}$</td>
</tr>
</tbody>
</table>

In this respect, Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$, Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ and Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ have been synthesized by hydrothermal reaction in a reflux system and a pressure reactor from pure metal chlorides at about 100 °C. We are also interested in the study of the onset of single domain structure as a function of particle size and how it relates to the observed properties such as coercive fields, magnetization and exchange bias effects. The particle sizes can be modified by milling and by thermal annealing of the as-prepared samples [6, 79]. Reliable values of the particle sizes are therefore necessary. We have obtained these from the measurements of X-ray diffraction (XRD), transmission electron microscopy (TEM).

In the next chapter we explore some details of the origin and different varieties of
magnetic order in solids. The basic principles of Mössbauer spectroscopy technique are reviewed in chapter 3. The experimental details are presented in chapter 4. In chapters 5, 6, 7 and 8 we present the results and discussions and finally the general conclusions are provided in chapter 9.
Chapter 2

Magnetism and magnetic order in solids

2.1 Introduction

There are various forms of magnetism that arise depending on how the magnetic dipoles interact with each other. In this chapter we discuss the different types of magnetic order in solids and review the most important concepts. These concepts are helpful in understanding and interpreting the experimental data of the materials under investigation in chapters 5 to 8. For detailed discussions of the varieties of Magnetic order in Solids, the reader is referred to a classical review by Hurd [29] and more recent books [80, 81]

2.2 Origin of magnetic moments

It is well known that moving electrical charges produce magnetic fields. This is a universal phenomenon that occurs for charges moving in a wire or for electrons orbiting a nucleus. To understand the existence of magnetic moments in solids, an analysis of the atomic structure is needed. Each electron in an atom has associated magnetic moments that originate from two sources. One is related to orbital motion around the nucleus and the other is its intrinsic spin. Being a moving charge, an electron may be
considered to be a small current loop which gives rise to orbital magnetic moments. The other magnetic moment originates from the intrinsic spin which can be spin up or down with respect to the direction of motion [82]. Both situations are illustrated in Figure 2.1. It is easy to show the link between magnetic moment and angular momenta of the electrons. Spin angular momentum usually dominates orbital angular momentum in determining the magnetic properties of a material [82]. In the following lines we are going to illustrate the existence of a magnetic moment due to an electron orbiting around the nucleus. An electron of mass $m_e$ moving in a closed orbit of radius $r$ would generate a current $I$ associated with a magnetic moment defined as

$$
\mu = IA \quad (2.2.1)
$$

where $A$ is the area of the closed loop with a magnitude of $\pi r^2$. If the electron with charge $(-e)$ moves at a frequency $f$ (with an angular speed $\omega = 2\pi f$) then

$$
I = -ef = \frac{e\omega}{2\pi}. \quad (2.2.2)
$$
The orbital magnetic moment can be written as

\[ \mu = -\frac{e r^2}{2} \omega = -\frac{em_e r^2}{2m_e} \omega = -\frac{e}{2m_e} l_z \quad (2.2.3) \]

where \( l_z \) is the orbital angular momentum given by \( m_e r^2 \omega \). In Quantum Mechanics, \( l_z \) is quantized in terms of the Planck’s constant \( \hbar = \frac{\hbar}{2\pi} \) \((l_z = m_l\hbar \text{ where } m_l = 0, 1, 2, 3 \ldots)\). The \( z \)-component of the orbital moment can be expressed as

\[ \mu_z = -\left( \frac{e\hbar}{2m_e} \right) m_l = \mu_B m_l. \quad (2.2.4) \]

The most fundamental unit for magnetic moments is known as the Bohr magneton \( \mu_B \), which is defined as \( \mu_B = \frac{e\hbar}{2m_e} = 9.274 \times 10^{-24} \text{ J/T} \). Similarly, the resultant spin momentum is given by \( \mu_S = -g_S \mu_B m_s \), where \( g_S = 2.0023 \). Spin magnetic moments may only be in up or in down directions with spin quantum numbers \( m_s = \pm \frac{1}{2} \). The net magnetic moment for an atom is just the sum of the magnetic moments of each of the constituent electrons, including both orbital and spin contributions and taking into account moment cancellations. For light elements, like 3d-metals, according to the Hund’s rules and Russel-Saunders coupling [82], first the orbiting electrons produce a resultant angular momentum

\[ \vec{L} = \sum_{i=1}^{n} \vec{l}_i. \quad (2.2.5) \]

Similarly the spin angular momentum of the electrons of a light atom couple to give a resultant spin momentum

\[ \vec{S} = \sum_{i=1}^{n} \vec{s}_i. \quad (2.2.6) \]

Both quantities \( \vec{L} \) and \( \vec{S} \) are required to minimize the atomic energy. The total angular momentum \( \vec{J} \) of an atom is taken as the coupling of \( \vec{L} \) and \( \vec{S} \) through spin-orbit interaction [82, 83]. Using Hund’s rules, the magnitude of the magnetic moment of an atom can be shown to be

\[ \mu_J = \mu_B g \sqrt{J(J+1)}, \quad (2.2.7) \]
where the \( g \) factor is defined by
\[
g = 1 + \frac{J (J + 1) + S (S + 1) - L (L + 1)}{2 J (J + 1)},
\]
(2.2.8)
for a free atom [82, 83]. For an atom having completely filled electron shells or subshells, when all electrons are considered, there is total cancellation of both orbital and spin moments. Thus, materials composed of atoms having completely filled electron shells will not have permanent magnetic moments.

### 2.3 Magnetization and susceptibility

The magnetization \( \vec{M} \) of a material is defined as the total magnetic moment per unit volume of a sample and can be expressed as
\[
\vec{M} = \frac{1}{V} \sum_{i=1}^{N} \vec{\mu}_i.
\]
(2.3.1)
This is a magnetic field dependant quantity which is sensitive to the temperature and the coupling between the magnetic moments. It is usually more convenient to express this physical quantity in terms of the mass of the sample because during measurements the volume of a sample may change due to thermal expansion and magnetostriction effects [83]. We can therefore write the magnetization per unit mass as
\[
\vec{\sigma} = \frac{1}{m} \sum_{i=1}^{N} \vec{\mu}_i.
\]
(2.3.2)
In the presence of an external applied magnetic field \( H \), the magnetic moments within a material will tend to become aligned with the field and to reinforce it. We can then determine the magnetization experimentally. The magnetic flux strength and the flux density are related according to the equation
\[
\vec{B} = \mu \vec{H}.
\]
(2.3.3)
where \( \mu \) is the permeability of free space and \( \vec{B} \) is the magnetic induction or magnetic flux density. The magnitude of \( \vec{M} \) is proportional to the applied field as follows

\[
\vec{M} = \chi \vec{H}
\]  

(2.3.4)

and \( \chi \) is called the magnetic susceptibility. The susceptibility of a material represents the degree to which a material responds to an external applied magnetic field. It helps to classify materials of various types in broad groups. Materials with a negative susceptibility are called diamagnetic as shown in Figure 2.2 [83]. Other types of magnetic order exist which have a wide range of susceptibilities and are illustrated in Figure 2.3 [83].

Figure 2.2: Graph of magnetic susceptibility versus temperature for a diamagnetic material.
Figure 2.3: Variation of inverse magnetic susceptibilities with temperature for paramagnetic, ferromagnetic and antiferromagnetic materials.

2.4 Magnetic order

As we have stated previously, the magnetic susceptibility, $\chi$ is a useful property for characterising magnetic materials. Its temperature dependence (usually the inverse of the susceptibility) is a good characterization parameter. In the next sections, we discuss the different types of magnetic order that occur in solids in more detail.

2.4.1 Diamagnetism

Diamagnetism is a very weak form of magnetism that is non-permanent and persists only while an external field is being applied on a sample. It is induced by a change in the orbital motion of all electrons due to applied magnetic fields. The magnitude of the induced magnetic moment is extremely small and is in a direction opposite to that of the applied field. Figure 2.4 illustrates schematically the atomic magnetic dipole configurations for a diamagnetic material with and without an external field [84]. Here,
the arrows represent induced atomic dipole moments. Diamagnetism is found in all materials. But because it is so weak, it can be observed only when other types of magnetism are not so large. Typical values of the diamagnetic susceptibility are of the order $-10^{-6}$ to $-10^{-5}$ [83].

![Figure 2.4: The atomic dipole configuration for a diamagnetic material with and without a magnetic field.](image)

### 2.4.2 Paramagnetism

For some solid materials, each atom possesses a permanent magnetic moment by virtue of incomplete cancellation of electron spin and orbital magnetic moments. In the absence of an external magnetic field, the orientations of these atomic magnetic moments are random, such that the material possesses no net macroscopic magnetization. These atomic moments are free to rotate. Paramagnetism results when the moments preferentially align by rotation with an external field as shown in Figure 2.5. In the presence of a magnetic field $B_0$, magnetic moments will orient themselves in particular directions with possible energies

$$E_J = -\vec{\mu}_J \cdot \vec{B}_0 = -g m_J \mu_B B_0,$$

(2.4.1)

where $m_J$ is the magnetic quantum number with values in range $-J < m_J < J$.

In equilibrium, the probability for the occupation of each energy level $E_{m_J}$ is given by
the Maxwell-Boltzmann distribution [84]

\[ P(E_J) = \frac{e^{-g\mu_B m_J B_0/k_B T}}{\sum e^{-g\mu_B m_J B_0/k_B T}}, \] (2.4.2)

where \( k_B \) is the Boltzman constant. We can show that the average magnetic moment is given by

\[ <\mu_B> = g\mu_B J F(J, x), \] (2.4.3)

where \( F(J, x) \) is the Brillouin function defined as

\[ F(J, x) = \left(1 + \frac{1}{2J}\right) \coth \left[\left(1 + \frac{1}{2J}\right)x\right] - \frac{1}{2J} \coth \left(\frac{x}{2J}\right). \] (2.4.4)

For \( n \) non-interacting magnetic moments per unit volume, the magnetization becomes

\[ M = n<\mu_B> = n g\mu_B J F(J, x). \] (2.4.5)

The parameter \( x \) is a dimensionless ratio of the Zeeman energy to the thermal energy given by

\[ x = \frac{g\mu_B J B_0}{k_B T}. \] (2.4.6)

For high temperature (\( T \sim 300 \) K) and low field (\( B_0 \sim 1 \) T), \( x \) becomes very small (\( x \ll 1 \)) such that the Brillouin function is approximated by

\[ F(J, x) \simeq \frac{x(J+1)}{3J}. \] (2.4.7)
This gives

\[ M = \frac{ng^2\mu_B^2J(J+1)B_0}{3k_B T}. \]  

(2.4.8)

Since the susceptibility is given by

\[ \chi = \frac{\mu_0 M}{B_0} \]  

(2.4.9)

and when substituting for \( M \) we get

\[ \chi = \frac{n\mu_0 g^2\mu_B^2J(J+1)}{3k_B T} = \frac{C}{T}. \]  

(2.4.10)

This is known as the Curie law for susceptibility where

\[ C = \frac{n\mu_0 g^2\mu_B^2J(J+1)}{3k_B} \]  

(2.4.11)

and \( C \) is called the Curie constant. However, when interactions between magnetic moments occur the Curie law is modified to the Curie-Weiss law expressed as

\[ \chi = \frac{C}{T - \theta_p}. \]  

(2.4.12)

\( \theta_p \) is known as the paramagnetic Curie temperature.

### 2.4.3 Ferromagnetism

Some materials with permanent magnetic moments and strong interaction between them show spontaneous magnetization even in the absence of an applied magnetic field. This occurs in a wide range of materials which include some alloy and pure metals like Fe, Co, Ni and Gd [83–85]. Magnetic susceptibilities are very high for ferromagnetic materials compared to that of paramagnets typically \( \chi_{FM} \sim 10^5 \chi_{para} \) [83].

Permanent magnetic moments in ferromagnetic materials result from atomic magnetic moments of electrons in different orbits of constituent atoms. In ferromagnetic materials, coupling interactions cause the magnetic moments of adjacent atoms to align with
one another, even in the absence of an external field. This is schematically illustrated in Figure 2.6. The order is perfect at absolute zero temperature. Increasing the thermal energy of the magnetic moments results in spin disorder due to thermal agitation. At the Curie temperature $T_C$ the disorder of magnetic moments becomes complete. For $T > T_C$, a ferromagnet exhibits properties of a paramagnet with a susceptibility that obeys the Curie-Weiss law. However, the law fails in the vicinity of $T_C$ where critical phenomena apply. The susceptibility near $T_C$ is approximated by $\chi \sim (T - T_C)^{-\gamma}$ when approaching $T_C$ from above and $\chi \sim (T_C - T)^{\beta}$ when approaching $T_C$ from below. The parameters $\gamma$ and $\beta$ are called critical exponents and are calculated to be 1 and 0.5 respectively in the so-called mean-field approximation [86]. A strong internal magnetic field $B_m$ is assumed to be responsible for aligning up magnetic moments. The spontaneous magnetization that results is taken to be proportional to $B_m$ such that

$$B_m = \lambda M_s$$

(2.4.13)

where $\lambda$ is referred to as the molecular field coefficient. The positive exchange interactions introduced in Quantum Mechanics are known to be responsible for the existence of $B_m$. The strength of the internal field can be roughly estimated from the magnetic
binding energy $\mu_B B_{in}$ and the thermal energy $k_B T_C$. The magnetic binding energy is responsible for the perfect alignment of moments at $T = 0$ K. At $T_C$ where the magnetic order collapses we expect

$$B_{in} \sim \frac{k_B T_C}{\mu_B}. \quad (2.4.14)$$

$B_{in}$ turns out to be much larger than the field that can be produced due to dipole fields of a permanent magnet. In the presence of external applied magnetic field $B_0$, the effective magnetic field in a sample is expressed by

$$\vec{B}_{\text{eff}} = \vec{B}_0 + \vec{B}_{in} = \vec{B}_0 + \lambda \vec{M}_s. \quad (2.4.15)$$

From equation 2.4.5 the magnetization of a ferromagnet in a applied field can be expressed as

$$M_s(B_0, T) = n g \mu_B J \ F(J, y) \quad (2.4.16)$$

where the ratio of the Zeeman energy to thermal energy is now defined as

$$y = \frac{g \mu_B J (B_0 + \lambda M_s)}{k_B T}. \quad (2.4.17)$$

The magnetization still stays finite even for $B_0 = 0$ since $B_{in} \gg B_0$. At absolute zero temperature ($T = 0$ K), the spontaneous magnetization per unit volume saturates to

$$M_s(0, 0) = n g \mu_B J. \quad (2.4.18)$$

For zero applied field ($B_0 = 0$) and $T > 0$, the reduced spontaneous magnetization of a ferromagnet can be expressed by

$$\frac{M_s(0, T)}{M_s(0, 0)} = F(J, y) \quad (2.4.19)$$

From this equation we can also expressed the reduced magnetization as

$$\frac{M_s(0, T)}{M_s(0, 0)} = \left( \frac{k_B T}{n g^2 \mu_B^2 \lambda J^2} \right) y. \quad (2.4.20)$$
where in this case $y$ is given by

$$y = \frac{g \mu_B J \lambda M_s (0, T)}{k_B T}. \quad (2.4.21)$$

The ferromagnetic state of a material can therefore be uniquely be described by satisfying two simultaneous equations 2.4.19 and 2.4.20.

2.4.4 Antiferromagnetism

Strong interaction between magnetic moments can give rise to antiparallel adjacent alignments. This is known as antiferromagnetic order. This occurs below the Néel temperature, $T_N$. Manganese oxide (MnO) is one material that displays this behavior which has ionic character, having both Mn$^{2+}$ and O$^{2-}$ ions. No net magnetic moment is associated with the O$^{2-}$ ions. The Mn$^{2+}$ ions possess a net magnetic moment that is predominantly of spin in origin. These Mn$^{2+}$ ions are arrayed in the crystal structure such that the moments of adjacent ions are antiparallel. This arrangement is represented schematically in Figure 2.7 [86, 87]. The opposing magnetic moments cancel one another and as a consequence, the solid as a whole possesses no net magnetization. The antiparallel alignment of moments is due to negative exchange interactions

![Figure 2.7: Magnetic structure in an antiferromagnet.](image)
between moments and is observed only below the critical temperature \( T_N \). The antiferromagnetic crystal can be divided into two atomic sublattices \( A \) and \( B \). Below \( T_N \) the net saturation magnetization of an antiferromagnet is zero due to the moments that are aligned antiparallel. If the temperature is increased above absolute zero temperature \( (T = 0 \text{ K}) \), saturation magnetization in each sublattice decreases with increase in temperature as in a ferromagnet \([86]\). At \( T_N \), the magnetic moments become randomly oriented and the paramagnetic phase starts. Using the mean-field theory and the assumption that an internal field \( B_{in} \) exists as in a ferromagnetic, the internal magnetic fields at the respective sublattices can be written as \([85, 86]\)

\[
\vec{B}^A_{in} = \lambda_{AA} \vec{M}_A + \lambda_{AB} \vec{M}_B \quad (2.4.22)
\]

and

\[
\vec{B}^B_{in} = \lambda_{BA} \vec{M}_A + \lambda_{BB} \vec{M}_B, \quad (2.4.23)
\]

where \( \vec{M}_A \) and \( \vec{M}_B \) are the sublattice magnetizations. The molecular field coefficients \( \lambda_{AB} \) and \( \lambda_{BA} \) correspond to the first nearest neighbors. The second nearest neighbors molecular field coefficient are given by \( \lambda_{AA} \) and \( \lambda_{BB} \) respectively. The internal field assumed to be dominated by interactions between first and second nearest neighbors. We also expect

\[
\lambda_{AB} = \lambda_{BA} = -\lambda_1 \quad (2.4.24)
\]

and

\[
\lambda_{AA} = \lambda_{BB} = \lambda_2 \quad (2.4.25)
\]

where \( \lambda_1 \) and \( \lambda_2 \) are both positive constants. Therefore, equations \((2.4.22)\) and \((2.4.23)\) can be rewritten in the form of

\[
\vec{B}^A_{in} = \vec{M}_A (\lambda_1 - \lambda_2) \quad (2.4.26)
\]

and

\[
\vec{B}^B_{in} = \vec{M}_B (\lambda_1 - \lambda_2) \quad (2.4.27)
\]
respectively. If we assume that the average magnetizations on A and B sublattices are $M_A = \frac{n}{2} < \mu_A >$ and $M_B = \frac{n}{2} < \mu_B >$, using equation (2.4.3) we can re-write the sublattice magnetizations as

$$M_A = \frac{n}{2} J g \mu_B F(J, y_A) \quad (2.4.28)$$

and

$$M_B = \frac{n}{2} J g \mu_B F(J, y_B) \quad (2.4.29)$$

where

$$y_A = \frac{J g \mu_B B_{in}^A}{k_B T} = \frac{J g \mu_B M_A (\lambda_1 - \lambda_2)}{k_B T} \quad (2.4.30)$$

and

$$y_B = \frac{J g \mu_B B_{in}^B}{k_B T} = \frac{J g \mu_B M_B (\lambda_1 - \lambda_2)}{k_B T} \quad (2.4.31)$$

If the magnetizations on the two sublattices are the same ($M_A = M_B = M$) we get

$$M = \frac{n J g \mu_B F(J, y)}{2} \quad (2.4.32)$$

At $T = T_N$, the magnetization becomes zero at each sublattice as in the case of a ferromagnet at $T_C$. We can easily show that $T_N$ can be expressed by

$$T_N = \frac{n g^2 \mu_0 \mu_B^2 J (J + 1)}{2 k_B \mu_0} = \frac{(\lambda_1 - \lambda_2) C}{2 \mu_0} \quad (2.4.33)$$

where $C$ is the Curie constant as before.

For $T > T_N$, the magnetization on each sublattice also depends on the applied external field $B_0$ such that the effective field on A and B sublattices is given by

$$\vec{B}_{eff}^A = \vec{B}_0 + \vec{B}_{in}^A = \vec{B}_0 - \lambda_2 \vec{M}_A - \lambda_1 \vec{M}_B \quad (2.4.34)$$

and

$$\vec{B}_{eff}^B = \vec{B}_0 + \vec{B}_{in}^B = \vec{B}_0 - \lambda_1 \vec{M}_A - \lambda_2 \vec{M}_B \quad (2.4.35)$$
respectively. We can also show that the susceptibility above $T_N$ obeys the Curie-Weiss law written as

$$\chi = \frac{C}{T - \theta_p},$$  \hspace{1cm} (2.4.36)

where

$$\theta_p = -\frac{C (\lambda_1 + \lambda_2)}{2\mu_0}.$$  \hspace{1cm} (2.4.37)

$T_N$ and $\theta_p$ are therefore related as follows

$$\theta_p = -\frac{(\lambda_1 + \lambda_2) T_N}{\lambda_1 - \lambda_2}.$$  \hspace{1cm} (2.4.38)

In the temperature range below $T_N$, the magnetic response of an antiferromagnetic material depends on the direction of the applied field $B_0$. The magnetization depends on whether the field is applied parallel or perpendicular to the alignment of the magnetic moments. This leads to parallel $\chi_\parallel$ and $\chi_\perp$ susceptibilities [86]. In powdered or poly-crystalline samples the average total susceptibility below $T_N$ is given by [86]

$$\chi = \frac{1}{3} \chi_\parallel + \frac{2}{3} \chi_\perp.$$  \hspace{1cm} (2.4.39)

\subsection*{2.4.5 Ferrimagnetism}

Some ceramics also exhibit a permanent magnetization, termed ferrimagnetism. The macroscopic magnetic characteristics of ferromagnets and ferrimagnets are similar. The distinction lies in the source of the net magnetic moments. The principles of ferrimagnetism are illustrated with the cubic ferrites. Ferrimagnetism is known to be an intermediate magnetic state between ferromagnetism and antiferromagnetism and can be described using the two sublattice theory due to Néel [88]. The net magnetization can be written as

$$M = \lambda M_A - (1 - \lambda) M_B,$$  \hspace{1cm} (2.4.40)

where $M_A \neq M_B$ as indicated in Figure 2.8. When $M_A = M_B$ we define the ferromag-
netic state corresponding to $\lambda = 0$ or 1 and antiferromagnetic state for $\lambda = \frac{1}{2}$. The ferrimagnetic state occurs when $\lambda \neq 0, \frac{1}{2}$ or 1. In ferrimagnets, the net magnetization is always non-zero for $T < T_C$ except in the special case when the magnetizations of the two sublattices may cancel out at a compensation temperature point $T_{\text{comp}} < T_C$.

### 2.4.6 Superparamagnetism

Superparamagnetism is a form of magnetism which appears in small ferromagnetic or ferrimagnetic nanoparticles. The magnetization of each particle can randomly point and flip in directions under the influence of temperature. The average time between flips is called the Néel relaxation time. In the absence of an external magnetic field and when the time used to measure the magnetization of the nanoparticles is much longer than the Néel relaxation time the magnetization of the sample averages to zero. Superparamagnets respond to an external magnetic field in a similar way to a paramagnet but the magnetic susceptibility in this case is much larger [83]. Because of the nanoparticle’s magnetic anisotropy, the magnetic moment has usually only two stable orientations which are antiparallel to each other and separated by an energy barrier. The stable orientations define the nanoparticle’s so-called “easy axes”. At a finite temperature, there is a finite probability for the magnetization to flip and reverse.
its direction. For a particle of volume $V$ the Néel relaxation time $\tau_N$ is expressed by Néel-Arrhenius equation [88]

$$\tau_N = \tau_0 \exp \left( \frac{KV}{\kappa B T} \right), \quad (2.4.41)$$

where $\tau_0$ is a length of time that is characteristic of the material called the attempt time or attempt period and $\kappa$ is the nanoparticle’s magnetic anistropy energy density. $KV$ is therefore the energy barrier associated with the magnetization flipping from its initial easy axes direction through a “hard plane”, to another easy axes direction. Measurement of the magnetization of a nanoparticle can be made in a finite time $\tau_m$. If $\tau_m \gg \tau_N$, the nanoparticle’s magnetization will flip several times during the measurement and the measured magnetization will average to zero. If $\tau_m \ll \tau_N$, the magnetization will not flip during the measurement so the measured magnetization will be what the instantaneous magnetization was at the beginning of the measurement. In the former case, the nanoparticle will appear to be in a superparamagnetic state whereas in the latter case it will appear to be “blocked” in its initial state. The measurement time of the magnetization is therefore critical. The transition between superparamagnetism and blocked state occurs when $\tau_m = \tau_N$ at a temperature called the superparamagnetic blocking temperature $T_{SPB}$ [34, 89]. Experimentally, superparamagnets do not show hysteresis in the variation of their isothermal magnetization as a function of applied magnetic field [29]. The superparamagnetic state vanishes with the reduction in temperature. The magnetization curve shows a rapid transition with decreasing temperature of the sample. A transition temperature $T_B$ called the blocking temperature can be defined which increases with increasing particle size [90]. In the superparamagnet region $T_B < T_C$, the magnetization response of the particles under the influence of an applied field $H$ is given by [29, 90, 91], [92]

$$\frac{M(T)}{M_S(0)} = \coth \left( \frac{\mu H}{k_B T} \right) - \frac{k_B T}{\mu H} = \frac{L(\frac{k_B T}{\mu H})}{(2.4.42)}$$
where $L$ is the Langevin’s function and $\mu$ is the moment of the superparamagnetic particle. Due to the collective excitations, the magnetizations of the nanoparticles can be expressed as $[91, 93]$

$$M(T) \approx M_S(0)\left(1 - \frac{k_B T}{2K V}\right). \quad (2.4.43)$$

### 2.5 Magnetic interactions

Magnetic moments in a solid can interact through two mechanisms namely dipole-dipole and exchange interactions. The dipole-dipole interactions can be shown to be too small to account for the origin of spontaneous magnetization. Exchange interactions which have Quantum Mechanical origin are responsible for the observed magnetic order. Magnetic moments that are so close that their wavefunctions overlap interact through direct exchange interaction. This interaction between magnetic moments with spins $\vec{S}_i$ and $\vec{S}_j$ can be expressed by the Heinsberg hamiltonian $[94]$

$$H_e = -J_{ij}\vec{S}_i \cdot \vec{S}_j, \quad (2.5.1)$$

where $J_{ij}$ is called the exchange integral which is positive for parallel aligned spins (ferromagnets) and negative for antiparallel aligned spins (antiferromagnets). Indirect exchange occurs through an intermediary when the interacting magnetic moments are far from each other. In metallic systems, the conduction electrons can act as intermediaries. This type of interaction is called the RKKY interaction named after Ruderman, Kittel, Kasuya and Yoshida $[94]$. In magnetic insulators, distant magnetic moments can interact through non-magnetic ions. This indirect exchange interaction is called superexchange interaction $[95]$. 

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2.5.1 Magnetic domain structure

Any ferromagnetic or ferrimagnetic material that is at a finite temperature \( T \) below \( T_C \) is composed of small regions called domains in which there is a mutual alignment of magnetic moments in the same direction as illustrated in Figure 2.9 [88]. Each domain is magnetized to its saturation magnetization. Adjacent domains are separated by domain boundaries or walls across which the direction of the magnetization gradually changes. Domains are usually microscopic in size and for a polycrystalline specimen, each crystalline grain, in general, consists of more than a single domain [95]. Thus in a macroscopic piece of material, there will be a large number of domains and all may have different magnetization orientations giving rise to a zero net magnetization of the sample. When an external field \( H \) is applied, the domains change in shape and size by the movement of domain boundaries. Schematic domain structures are represented in the insets (labeled U through to Z) at several points along the \( B \) versus \( H \) curve in Figure 2.10 [96]. Initially, the moments of the constituent domains are randomly oriented such that there is no net \( B \) (or \( M \)) field (inset U). The domains that are oriented in directions favorable to the applied field grow at the expense of those that...
are unfavorably oriented (insets V through X). This process continues with increasing field strength until the macroscopic specimen becomes a single domain, which is nearly aligned with the field (inset Y). Saturation is achieved when this domain, by means of rotation, becomes oriented with the $H$ field (inset Z).

![Figure 2.10: The $B$ versus $H$ behavior for a ferromagnetic or ferrimagnetic material that was initially unmagnetized.](image)

### 2.6 Magnetization process

The magnetization process of a sample is influenced by both external influences and internal microstructure and can be explained by rotation of magnetic moments or by displacement of domain walls. The magnetization characterizes the order of the moments in response to both applied and internal fields. If we assume that a magnetically ordered material consists of domains and domain walls, in the presence of external
fields the magnetization is uniform in the domains and non-uniform in the domain walls. The principal measurements encountered here will involve isothermal measurements of magnetization as a function of applied magnetic field and are presented in the form of a hysteresis loop as shown in Figure 2.11 [96]. From a magnetization point S

![Figure 2.11: Variation of magnetization with applied field in a ferromagnet.](image)

in Figure 2.11, as the field $H$ is reduced, the curve does not retrace its original path. A hysteresis effect is produced in which the magnetization $M$ lags behind the applied field $H$. At zero field (point R on the curve), there exists a residual field $M_r$ that is called the remanence. Here the material remains magnetized in the absence of an external field. Upon reversal of the field direction from saturation, the process by which the domain structure changes is reversed. First, there is a rotation of the single domain with the reversed field. Next, domains having magnetic moments aligned with the new field will grow at the expense of the former domains [96]. To reduce the magnetization within the specimen to zero, a field of magnitude $-H_C$ must be applied in a direction opposite to that of the original field. $H_C$ is called the coercivity, or simply the coercive
field. Upon continuation of the applied field in this reverse direction, as indicated in the figure, saturation is ultimately achieved in the opposite sense, corresponding to point $S'$. A second reduction of the field to the point of the initial saturation (point S) completes the symmetrical hysteresis loop and also yields both a negative remanence ($-M_r$) and a positive coercivity ($+H_C$). The approach to saturation of the initial magnetization curve can be approximated by an empirical relationship of the form

$$M(H) = M_s(0) \left(1 - \frac{a}{H} - \frac{b}{H^2} - \ldots\right) + \chi H$$

(2.6.1)

where $a$ and $b$ are fit parameters and $\chi$ is the high-field susceptibility [96, 97]. The study of the hysteresis loop is important as it provides information about the domain wall movements. The bigger the coercive fields the harder it is to reverse the magnetization. From the hysteresis curve we can be able to distinguish between soft and hard magnets. In this work we will also give particular attention to the evolution of the coercive field with particle size.

### 2.7 Exchange bias

When a sample contains an interfaces between ferromagnetic, ferrimagnetic and antiferromagnetic phases is subjected to a magnetic field reversal, it may exhibit an additional unidirectional anisotropy due to magnetic coupling at the interface. This effect, called exchange bias (EB), was first discovered nearly 50 years ago in oxidized Cobalt nanoparticles [98]. Exchange bias has also been observed in many other magnetic materials. Although there has been some research in exchange bias in nanoparticles in the last decades, the bulk of exchange bias research has focused mainly on thin film systems [98].
2.7.1 Basic phenomenology of exchange bias

The phenomenology of exchange bias has been extensively described in different reviews published on the subject, [98–100]. The main indication of the existence of exchange bias is the shift of the hysteresis loop, $H_{EB}$, along the field axis after field cooling from above the Néel temperature, $T_N$, of the AFM (and below the Curie temperature, $T_C$, of the FM) in materials composed of FM-AFM interfaces. The transition from a shifted to a centred loop appears close to the Néel temperature of the AFM phase, confirming that it is the presence of the antiferromagnetic material which causes the exchange bias effect. In most systems, the horizontal shift is opposite to the cooling field direction and is therefore called negative exchange bias. Generally, the exchange bias field does not depend markedly on the amplitude of the cooling field. However, studies of FeF$_2$/Fe and MnF$_2$ [100] bilayers revealed a rather unusual behaviour. For large cooling fields the loops, instead of shifting towards negative fields (when cooled in a positive field), shifted to positive fields, i.e. in the same direction as the cooling field. This effect is then called positive exchange bias. Different theoretical models have been proposed to explain this effect [100, 101] which are all based on the existence of an antiferromagnetic coupling at the interface between the FM and the AFM layers. Note that for conventional negative exchange bias a ferromagnetic interfacial coupling has usually been assumed. Independent of the direction of the horizontal shift of the hysteresis loop, it is always accompanied by an increase of the coercivity $H_c$ below the exchange bias blocking temperature $T_{EB}^B$ which is linked to the anisotropy of the AFM layer. However, the coercivity is also affected by the thicknesses and microstructures of the FM and AFM layers. This increase of $H_c$ is intuitively simple to understand. For an AFM with small anisotropy, when the FM rotates, it drags the AFM spins irreversibly, hence increasing the FM coercivity. For a large AFM anisotropy, the FM decouples because it cannot drag AFM spins, consequently the coercivity is reduced. A
consequence of the influence of the anisotropy is a peak of coercivity that often appears close to $T_B$ and is due to the decrease of the AFM anisotropy close to $T_B$. The width of the peak is related to sample homogeneity which reflects the distribution of AFM anisotropies. An analogous peak effect is found in the AFM thickness dependence of $H_c$ [102]. The effective AFM anisotropy is reduced with thickness. For thin AFM films, the exchange bias effect as well as the increase of $H_c$ disappear. Figure 2.12 (a), shows an FM/AFM system at a temperature $T$ that is below the Curie temperature ($T_C$) of the ferromagnet and above the exchange bias blocking temperature $T_{EB}^B$ of the antiferromagnet ($T_B < T < T_C$). The hysteresis loop of the FM/AFM system at this temperature is equal to the hysteresis curve of the pure ferromagnet plus a small paramagnetic part from the AFM and is shown in 2.12 (b). The hysteresis loop is perfectly centred around the origin. The FM/AFM system is then cooled well below $T_B$ in the presence of a magnetic field $H$ (or in a state where the FM has a remanent magnetisation), which is usually aligned parallel to an easy axis of the FM 2.12 (d). The hysteresis loop of the FM/AFM system in this state is shifted along the field axis, generally in the direction opposite (negative) to the applied cooling field 2.12 (e). Additionally, the hysteresis loop shows a strong increase of the coercivity $H_C$. Figure 2.12 (c) shows a typical torque magnetometry curve of a ferromagnetic material with uniaxial anisotropy whereas a torque curve of an exchange biased FM/AFM system is shown in 2.12 (f). The uniaxial anisotropy of a ferromagnet gives rise to a $\sin 2\theta$ behaviour of the torque signal 2.12 (c), whereas the $\sin \theta$ behaviour of the FM/AFM system is a clear sign for a unidirectional anisotropy 2.12 (f). The energy functions of both systems are represented by the dotted lines in 2.12 (c) and 2.12 (f). It is apparent that in (c) two energy minima occur at $\theta = 0^\circ$ and $\theta = 180^\circ$ and in 2.12 (f) only one at $\theta = 0^\circ$ [101].
Figure 2.12: Comparison of the magnetic properties of an FM/AFM system at a temperature $T$ with $T_B < T < T_C$ (a), and the same system after field-cooling below the AFMs Néel temperature (d) (with $T < T_B < T_C$). The system (a) shows a normal ferromagnetic hysteresis loop (b) and an uniaxial anisotropy, indicated by a $\sin(2\theta)$ behavior of the torque measurements (d). System (d), after field cooling below $T_B$, shows a horizontally shifted loop with increased coercivity (e), and an unidirectional anisotropy with a $\sin\theta$ behaviour of the torque measurement.

### 2.7.2 Training effect

The training effect was first discovered in 1966 by Paccard et al. [103] shortly after the discovery of the exchange bias shift by Meiklejohn and Bean. This phenomenon is observed in FM/AFM systems when they are field cycled. In this case, the exchange bias field is found to vary with the number of hysteresis loops. If several consecutive hysteresis loops are measured, the shift $H_{EB}$ of consecutive loops will decrease. It can thus be characterised by the change of the switching fields, $H_{sw-}$ and $H_{sw+}$, with the
number of hysteresis cycles. $H_{sw-}$ ($H_{sw+}$) define the field at which the sample magnetisation switches from positive to negative (or negative to positive) values (see Figure 2.13). This empirical variation of the switching fields with the number of consecutive hysteresis loop measurements can be subdivided into three different types. In the first type of exchange biased systems called Type I, the hysteresis loop shrinks from both sides, which means $H_{sw-}$ increases and $H_{sw+}$ decreases. This behaviour of the switching fields corresponds to the one observed by Paccard et al. [103]. If both switching fields, $H_{sw-}$ and $H_{sw+}$ increase, the training effect is denoted as Type II [103]. It is not very surprising that an intermediate case between Type I and Type II systems was also found and is denoted as Type 0 training effect [101]. In Type 0 systems $H_{sw-}$ increases, as in Type I and II, and $H_{sw-}$ stays constant. This behaviour is mainly be observed in antiferromagnetic metallic systems such as FeMn and IrMn. The behaviour of Type I, II and 0 training effect in FM/AFM systems is illustrated in Figure 2.13 (a) to (c) respectively. For each Type, the first (red), the second (orange) and fifth (yellow) of the consecutively measured hysteresis loops are shown. Experimentally, it is often found that $H_{EB\infty} \propto 1/\sqrt{n}$ where $n$ indicates the order of consecutive loops measured. It is important to stress that the training effect is more important in antiferromagnetic polycrystalline samples and is very small or non-existent in systems based on single crystals [103].
Figure 2.13: Type I, II and 0 training effect for the first (red), second (orange) and the fifth (yellow) hysteresis loop measurement.
Chapter 3

Mössbauer Spectroscopy

3.1 Introduction

Mössbauer spectroscopy is a spectroscopic technique based on the Mössbauer effect discovered by Rudolf L. Mössbauer in 1957 [104]. The technique probes tiny changes in the energy levels of an atomic nucleus in response to its environment. Scientists in different fields such as Physics, Chemistry and Geology use these tiny energy changes to provide useful information about the chemical bonding, structure and magnetic properties of materials [104, 105]. Mössbauer spectroscopy has been widely used in the study of bulk as well as the surface properties of materials [106]. Mössbauer spectroscopy can also be used to study nanostructured materials. It can also provide information on dynamic properties such as superparamagnetic relaxation, diffusion and mechanical vibrations of Mössbauer isotopes in samples. Mössbauer spectroscopy is now a well established experimental technique in the investigation of solids. In a Mössbauer experiment a suitable radioactive source is used as a spectroscopic probing tool. This is achieved by changing the energy of the emission spectrum of the source with respect to that of the absorber (specimen) by moving the source towards and away from the absorber. This tunes the absorber in and out of resonance making it possible to scan through the different absorption lines and measure the hyperfine interactions. In this chapter we present some of the basic principles of the technique.
3.1.1 Mössbauer effect

The phenomenon of the emission or resonant absorption of gamma ray photons without loss of energy due to recoil and without thermal broadening is known as the Mössbauer effect. The important factors which must be considered in order to understand the physical basis of the Mössbauer effect and the importance of recoilless emission of gamma rays are discussed below.

3.1.1.1 Natural line width

Consider the emission of \( \gamma \)-ray photons from an atom corresponding to a transition to the ground state. The emitted gamma rays have a very small spread of energies. The uncertainty in energy corresponds to the width \( \Gamma \) of the nuclear state and can be obtained from the Heisenberg uncertainty relation

\[
\Delta E \cdot \Delta t \geq \hbar
\]  

(3.1.1)

where \( \hbar = \frac{\hbar}{2\pi} \) and \( \hbar \) is the Planck’s constant and \( \Delta t \) is the time interval to measure the energy \( E \) which is in the order of the meanlife \( \tau \) of the state under consideration. Weiskopf and Wigner showed [107] that by setting \( \Delta t \approx \tau \), the approximate width \( \Gamma = \Delta E \) of a level is given by \( \Gamma = \frac{\hbar}{\tau} \) where \( \Gamma \) represents the full width of the transition spectral line at half maximum. Further, Weidkopf and Wigner found that the spectral line has a Lorentzian or Breit-Wigner shape described by

\[
I(E) = \text{(constant)} \frac{\Gamma/2\pi}{(E - E_0)^2 + (\Gamma/2)^2}
\]  

(3.1.2)

where \( I(E) \) is the transition energy intensity and \( E_0 \) represents the most probable transition energy. The width of the transition line is governed by the mean lifetime \( \tau \) of the excited state. In Mössbauer spectroscopy, the lifetime of excited states range from \( \approx 10^{-6} \) to \( 10^{-11} \) s, and for \( ^{57}\text{Fe} \) the mean lifetime for the first excited Mössbauer state is \( \tau = 1.43 \times 10^{-7} \) s. The resulting value for the linewidth \( \Gamma \) is \( 4.55 \times 10^{-9} \) eV.
3.1.1.2 Nuclear resonance

When atoms are held tightly as in solids, the gamma radiation emitted by their nuclei are very close to being recoil-free. This corresponds to the transition energy between the nuclear ground state and the excited state. When the photon carrying the full nuclear transition energy strikes another identical nucleus also embedded in a tight crystalline structure, absorption may occur. Since the absorption in general can occur only for a nucleus in the ground state, only a $\gamma$-ray emitted in a transition to the ground state is useful for practical application of the Mössbauer effect. The principle of the Mössbauer effect is illustrated in Figure 3.1 [106]. If a spectral line for the emission and absorption processes coincide at the same energy position $E_0$, then the maximum resonance absorption occurs. The resonance absorption cross-section is given by the Breit-Wigner formula

$$\sigma = \frac{\sigma^0 \Gamma^2}{\Gamma^2 + 4(E - E_0)^2}$$

(3.1.3)

where $\sigma^0$ is the maximum cross-section and is given by

$$\sigma^0 = \frac{\lambda^2}{\pi} \frac{2I_e + 1}{2I_g + 1} \frac{1}{\alpha + 1}$$

(3.1.4)

where $I_e$ and $I_g$ are the nuclear spin quantum numbers for the excited and ground states, respectively. $\lambda$ is the wavelength of the $\gamma$-ray and $\alpha$ is the internal conversion
coefficient (for $^{57}\text{Fe}$, $\alpha = 8.21$). The nucleus remains in the excited state of energy $E_\circ$ for the mean lifetime after the absorption process and then undergoes a transition back to the ground state by emission of either a $\gamma$-ray or conversion electron due to internal conversion (the transfer of the photon energy to an electron in the innermost electron shells of the atom). This process is referred to as nuclear resonance fluorescence.

### 3.1.1.3 Recoil energy loss

Consider a $\gamma$-ray (photon) emitted from an excited nucleus of mass $M$ (initially at rest). This process gives rise to a recoil imparted to the emitting nucleus. As a result the nucleus moves in the opposite direction to the $\gamma$-ray emission with a velocity, say $\vec{v}$ as shown in Figure 3.2 [105, 106]. The kinetic recoil energy is given by $E = \frac{1}{2}Mv^2$. Applying the conservation of momentum to the above process gives

$$p_n = -p_\gamma = -\frac{E_\gamma}{c} \tag{3.1.5}$$

where $p_n$ and $p_\gamma$ are the linear momenta of the nucleus and the $\gamma$-ray, respectively and $E_\gamma = E_\circ - E_R$. Taking into consideration the large mass of the nucleus and using non-relativistic approximations gives

$$E_R = \frac{p_n}{2M} = \frac{E_\gamma^2}{2Mc^2}. \tag{3.1.6}$$

For $E_R \ll E_\circ$, we can set $E_\gamma \approx E_\circ$ in equation (3.1.6) which reduces to

$$E_R = \frac{E_\circ^2}{2Mc^2}. \tag{3.1.7}$$

Figure 3.2: Recoil energy $E_R$ received by an isolated nucleus on gamma ray emission or absorption.
Evaluating equation (3.1.7) into numerical form results in

\[ E_R(\text{eV}) = 5.37 \times 10^{-4} \frac{E_o^2}{A}, \]  

(3.1.8)

where \( A \) is the atomic mass of the decaying nucleus. For \(^{57}\text{Fe}\), the Mössbauer transition between the first excited state and the ground state \((E_o = E_e - E_g = 14.4 \text{ keV})\) results in \( E_R = 1.95 \times 10^{-3} \text{ eV} \).

### 3.1.1.4 Thermal broadening

During the decay process, the recoil effect causes a displacement from \( E_o \) by an amount \( E_R \) shown in Figure 3.3 [106]. In the absorption process, for the \( \gamma \)-ray to be absorbed by a nucleus requires a total energy of \( E_\gamma = E_o + E_R \) to make up for the transition from the ground state to the excited state and the recoil effect. The transition lines for absorption and emission are separated by \( 2E_R \), which is \( 10^6 \) times larger than the natural line width \((\Gamma = 4.55 \times 10^{-9} \text{ eV})\), as a result, the \( \gamma \)-ray emission line does not overlap the absorption line, and the nuclear resonance absorption is not observable.

The atoms of a gas are continuously in motion with large velocities. If \( \gamma \)-ray emission occurs while the nucleus (atom) is moving at a velocity \( v_n \) in the direction of \( \gamma \)-ray propagation then the \( \gamma \)-ray of energy \( E_\gamma \) receives a Doppler energy \( E_D \) given by

\[ E_D = \frac{v_n}{c} E_\gamma \]  

(3.1.9)

which is added to \( E_\gamma \)

\[ E_\gamma = E_o - E_R + E_D. \]  

(3.1.10)

The mean Doppler broadening can be determined from [106]

\[ \overline{E_D} = E_\gamma \left( \frac{2E_K}{Mc^2} \right)^{\frac{1}{2}} \]  

(3.1.11)

where \( E_k \) is the mean kinetic energy of the moving nucleus (or atom) given by

\[ E_K = \frac{1}{2} M v_n^2 = \frac{3}{2} k_B T. \]  

(3.1.12)
Consider an Einstein solid with $3N$ vibrational modes ($N$ is the number of atoms in the solid) each having the same frequency $\omega_E$. The solid is characterized by the quantum numbers of its oscillators and any changes in its state is a result of an increase or decrease in one or more of the quantum numbers. This corresponds to the absorption or emission of quanta of energy $\hbar \omega_E$ which in solids is of the order of $10^{-2}$ eV. The emission of $\gamma$-rays is accompanied by the transfer of integral multiples of this photon energy ($0\hbar \omega_E, \pm \hbar \omega_E, \pm 2\hbar \omega_E, ...$) to the lattice. Therefore, the fraction of events, $f$, which takes place without lattice excitation, provided $E_R \ll \hbar \omega_E$ is given by

$$E_R = (1 - f)\hbar \omega_E \tag{3.1.13}$$

and

$$f \approx 1 - \frac{E_R}{\hbar \omega_E} = 1 - k^2 < x^2 > \tag{3.1.14}$$

where $< x^2 >$ is the expectation value of the squared vibrational amplitude in the $x$-direction and $k$ is the propagation vector [108]. The above equation can be written
in the following general form

\[ f = \exp \left( -\frac{E_R}{\hbar \omega_E} \right) = \exp(-k^2 < x^2>). \] (3.1.15)

From the debye model for solids [106], the recoil-free fraction can be written as

\[ f = \exp \left[ -\frac{6E_R}{k_B\theta_D^2} \left\{ \frac{1}{4} + \left( \frac{T}{\theta_D} \right)^2 \int_0^{\theta/T} \frac{x}{e^x-1} \, dx \right\} \right]. \] (3.1.16)

For \( T \ll \theta_D \), the above equation reduces to

\[ f = \exp \left( -\frac{6E_R T}{k_B\theta_D^2} \right), \] (3.1.17)

where \( \theta_D = \hbar \omega/k_B \) is the Debye temperature. The recoil-free fraction, \( f \) is referred to as the Debye-Waller factor or Lamb-Mössbauer factor. This factor increases with decreasing recoil energy loss, \( E_R \), decreasing temperature, \( T \) and increases with increasing Debye temperature, \( \theta_D \). \( \theta_D \) may be considered as a measure of the strength of the bonds between Mössbauer atom and the lattice. The \( f \)-value for the 14.4 keV \( \gamma \)-transition in \( ^{57}\text{Fe} \) at 0 K can be determined from the above equations to be 0.91.

### 3.1.2 Hyperfine interactions

Hyperfine interactions are interactions between a nucleus and its surrounding environment that arise from the interactions between the static magnetic and electric moments of the nucleus with the electron charge and spin distributions in its immediate vicinity. These interactions influence the nuclear levels and thus also the transition energies, in a characteristic way and allow valuable information about the absorbing atom and its surrounding to be obtained. These include isomer shift (\( \delta \)), magnetic quadrupole interaction (\( \Delta \)) and magnetic hyperfine interaction (\( H \)) as illustrated in Figure 3.4 [106].
3.1.2.1 Isomer shift

The isomer shift of absorption lines in a Mössbauer spectrum arises due to the non-zero volume of the nucleus and the electron charge density due to s-electrons within it leading to an electric monopole (Coulomb) interaction which alters the nuclear energy levels. The volume of the nucleus in its ground and excited states are different and the s-electron densities are affected by the chemical environment. This relationship between s-electron density and nuclear radius is given by

\[
\delta = \frac{2}{5} \pi Z e^2 \left( |\varphi_s(0)|_E^2 - |\varphi_s(0)|_A^2 \right) \left( \langle R_s^2 \rangle - \langle R_s^2 \rangle \right)
\]  

(3.1.18)

where \( \langle R_s^2 \rangle \) and \( \langle R_s^2 \rangle \) are the mean square radii of the ground and excited state nuclear states, \( |\varphi_s(0)|_E^2 \) and \( |\varphi_s(0)|_A^2 \) are the electron densities at the emitting and absorbing nuclei and \( Z \) is the atomic number \([104, 105, 109]\). Any difference in the s-electron environment between emitter and absorber thus produces a shift in the resonance.
energy of the transition. This shift cannot be measured directly and so a suitable reference is necessary, such as a specific source or an absorber. The isomer shift is good for probing the valence state of the Mössbauer atom. As the wavefunctions of the s-electrons penetrate into outer shells, changes in these shells will directly alter the s-electron charge density at the nucleus. For example, Fe$^{2+}$ and Fe$^{3+}$ have electron configurations of (3d$^6$) and (3d$^5$) respectively. The ferrous ions have less s-electron density at the nucleus due to the greater screening of the d-electrons. This produces a positive isomer shift greater in ferrous iron than in ferric.

### 3.1.2.2 Quadrupole splitting

The existence of an electric quadrupole interaction is one of the most useful features of Mössbauer spectroscopy. The theory is closely related to that used in nuclear quadrupole resonance spectroscopy [104]. A nucleus that has a spin quantum number $I > \frac{1}{2}$ has a non-spherical charge distribution. The magnitude of the charge deformation, $Q$, is given by

$$
e Q = \int \rho r^2 (3\cos^2 \theta - 1) dr$$

(3.1.19)

where $e$ is the charge of the proton, $\rho$ is the charge density in a volume element $d^3 r$ at a distance $r$ from the center of the nucleus and making an angle $\theta$ to the nuclear spin quantisation axis. The sign of $Q$ indicates the shape of the deformation. Negative $Q$ is due to the nucleus being flattened along the spin axis, an elongated nucleus gives a positive $Q$. An assymetric charge distribution around the nucleus causes an assymetric electric field at the nucleus, characterised by a tensor quantity called the Electric Field Gradient (EFG), \( \nabla E \). The electric quadrupole interaction between these two quantities gives rise to a splitting in the nuclear energy levels. The interaction between nuclear moment and EFG is expressed by the Halmitonian

$$\overrightarrow{H_{Eg}} = -\frac{1}{6} e Q \nabla^2 \overrightarrow{E}$$

(3.1.20)
where $\nabla^2 E$ may be written as [108]

$$V_{ij} = \frac{\partial^2 V}{\partial x_i \partial x_j}$$  \hspace{1cm} (3.1.21)

$x_i, x_j = x, y, z$ where $V$ is the electrostatic potential. There are two contributions to EFG i) lattice contributions from charges on distant ions and ii) valence contributions due to incompletely filled electron shells. If a suitable coordinate system is chosen the EFG can be represented by three principal axes $V_{xx}$, $V_{yy}$ and $V_{zz}$, if an asymmetry parameter is defined using these axes as [104]

$$\eta = \left( \frac{V_{xx} - V_{yy}}{V_{zz}} \right)$$  \hspace{1cm} (3.1.22)

where $|V_{xx}| \geq |V_{yy}| \geq |V_{zz}|$ so that $0 \leq \eta \leq 1$. The EFG can be specified by two parameters: $V_{zz}$ and $\eta$. The Hamiltonian for the quadrupole interaction can be rewritten as

$$H_{Eq} = \frac{e^2 qQ}{4I(2I - 1)} \left[ 3I_z^2 - I(I + 1) + \frac{\eta(2I_z^2 + I_z^2)}{2} \right]$$  \hspace{1cm} (3.1.23)

where $I_+$ and $I_-$ are shift operators and $I_z$ is a spin operator [85, 109]. The excited state of $^{57}$Fe has a spin $I = 3/2$. The EFG has no effect on the $I = 1/2$ ground state but does remove degeneracy in the excited state, splitting it into two sub-states $m_I = \pm 1/2$ and $m_I = \pm 3/2$ states are higher in energy for positive $V_{zz}$. The energy eigenvalues for $I = 3/2$ have exact solutions given by

$$E_{Eq} = \frac{e^2 qQ}{4I(2I - 1)} \left[ 3m_I^2 - I(I + 1) \right] \left( 1 + \frac{\eta^2}{3} \right)^{1/2}$$  \hspace{1cm} (3.1.24)

whilst the energies for higher spin states require analytical methods to calculate the energies. The now non-degenerate excited states give rise to a doublet in the Mössbauer spectrum as illustrated in Figure 3.4. The separation between the lines, $\Delta$, is known as the quadrupole splitting and is given by

$$\Delta = \frac{e^2 qQ}{2} \left( 1 + \frac{\eta^2}{3} \right)^{1/2}$$  \hspace{1cm} (3.1.25)

with the lines intensities being equal for polycrystalline samples.
3.1.3 Magnetic Hyperfine Splitting

Magnetic hyperfine splitting is caused by the dipole interaction between the nuclear spin moment and a magnetic field i.e. Zeeman splitting. The effective magnetic field experienced by the nucleus is a combination of fields from the atom itself, from the lattice through crystal field effects and from external applied fields. This can be considered for now as a single field, $B$, whose direction specifies the principal, $z$ axis. The Hamiltonian for the magnetic hyperfine dipole interaction is given as

$$H = -\mu_B B = -g\mu_N I.B$$

(3.1.26)

where $\mu_N$ is the nuclear Bohr magneton, $\mu$ is the nuclear magnetic moment, $I$ is the nuclear spin and $g$ is the nuclear $g$-factor [85]. This Hamiltonian yields eigenvalues of

$$E_M = -g\mu_N B m_I$$

(3.1.27)

where $m_I$ is the magnetic quantum number representing the $z$ component of $I$ (where $m_I = I, I - 1, ..., -I$). The magnetic field splits the nuclear level of spin $I$ into $(2I+1)$ equispaced non-degenerate substates. This and the selection rule of $\Delta m_I = 0, \pm 1$ produces splitting and a resultant spectrum for a $3/2 \rightarrow 1/2$ transition in the case of $^{57}\text{Fe}$.
Chapter 4

Experimental techniques

4.1 Introduction

Mixed metal oxides can be produced by solid state reaction and high energy ball milling from high purity oxides. Wet chemical methods such as sol-gel [110], hydrothermal [25], [26], glycothermal [9], citrate precursor [82, 83] and combustion methods [8, 82, 83] can also be used to produce better quality materials from salt solutions. The samples studied here were made by using hydrothermal techniques. High energy ball milling was used to reduced the particle sizes of the samples. The single phase corundum structure in all the synthesized samples was confirmed by X-ray diffraction. The magnetic properties were studied using $^{57}$Fe Mössbauer spectroscopy, vibrating sample magnetometer (VSM) and superconducting quantum interference device (SQUID) magnetometer. The experimental procedures for synthesis and measurement of certain basic properties are presented in this chapter.

4.2 Hydrothermal Process

The hydrothermal process is one of the common techniques of synthesizing compounds from aqueous solutions of metal salts. The starting materials in this method are high-purity metal chlorides or nitrates and a precipitating reagent such as ammonia, sodium
hydroxide or potassium hydroxide. The stirring, reaction temperature, pressure and washing stage play important roles in obtaining homogeneous and single-phase crystallization of the compounds. We have prepared \((\text{Sn, Mn, Mg})_{0.2} \text{Cr}_{1.8-x} \text{Fe}_x \text{O}_3\) compounds by hydrothermal technique. The starting materials were \(\text{SnCl}_2 \cdot 6\text{H}_2\text{O}\) (99%), \(\text{MnCl}_2\) (99.99%), \(\text{MgCl}_2\) and \(\text{FeCl}_3 \cdot 6\text{H}_2\text{O}\) (99%) which were supplied by Sigma Aldrich.

The stoichiometric compositions were calculated to yield a target mass of 5.0 g. The chlorides were mixed in deionised water by a magnetic stirrer for about 30 minutes. The precipitation reagent were added drop-wise to the salt mixtures until complete precipitation. The precipitate was washed several times over Whatman GF/F microfiber filters by deionised water until all the chloride ions were removed as confirmed by using a standard solution of \(\text{AgNO}_3\). The precipitate was finally dispersed in about 400 ml of deionised water. The samples were synthesized in a model 4843 PARR pressure reactor as shown in Figure 4.1 or in an open glass reflux system at atmospheric pressure as shown in Figure 4.2 [111].

![Figure 4.1: The stirred pressure reactor with a PARR 4843 controller.](image)
The reactor was operated at a soak temperature of 100 °C for 3 hours at a stirring speed and pressure of 300 rpm and 120 psi respectively. The operating schedule and the set-up configurations of the PARR 4843 pressure reactor are shown respectively in Figure 4.3 and in Table 4.1 [111]. The cooled final product was finally filtered over fresh Whatman microfiber and rinsed with 200 ml of ethanol. The ethanol drives out the water from the sample and is easier to remove from the sample by drying. The synthesized oxides were dried under 250 W infrared light for 3 hours. The dried samples were homogenized into fine powder using an agate mortar and pestle. A typical mass of 4.73 g of the oxides was produced. The difference in the target mass and actual mass recorded was a result of some samples being lost during the synthesis process. The sample was finally sintered at 600 °C for 12 hours in order to achieve single phase formation.
Table 4.1: The general and special set-up configurations of the PARR 4843 controller for the pressure reactor.

(i) general fixed settings.

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(ii) Special variable settings.

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4.3 High-energy ball milling

High-energy ball milling is a simple and effective method for producing compounds and alloys by mechanical synthesis method. In this technique the required proportions of the starting materials are mixed and sealed in hardened steel vials with steel balls. Agents like stearic acid or acetone may be added to the mixture or simply dry milled [112]. The milling time required to form the sample depends on the ball to sample mass ratio, the speed at which the vials are rotated and ease of phase formation of the target material. We have used a Retsch planetary ball mill type PM 400 MA shown in Figure 4.4 for particle size reduction for some of our samples. This facility has four grinding stations and can be operated to a maximum speed of 300 rev/min. The recommended
speed is 200 rev/min for long grinding periods. The grinding environment consists of 250 ml hardened steel vials with an appropriate number of balls that depends on the sample size. We have used suitable covers of the vials available to allow for grinding in air or inert gas atmosphere. The ball to sample mass ratio used was 20:1. The sample size in each vial was about 2 g. A typical grinding schedule was for a total time of at least 4 hours at a speed of 200 rev/minute. At conveniently selected times (for example 1, 2, 3 and 4 hours) about 0.2 g of sample was removed in order to study the effect of particle size reduction [112].

Figure 4.4: Retsch PM 400 planetary ball mill used at the Condensed Physics laboratory, UKZN.

### 4.4 X-ray Powder Diffraction

X-ray powder diffraction (XRD) is a rapid analytical technique primarily used for phase identification of a crystalline material and can provide information on unit cell dimensions and quality of the sample. X-ray diffraction is based on constructive interference of monochromatic X-rays in a crystalline sample. These X-rays are generated by a cathode ray tube, filtered to produce monochromatic radiation, collimated to concen-
trate, and directed towards the sample. The interaction of the incident rays with the sample produces constructive interference when the condition for Bragg’s law

\[ n\lambda = 2d\sin\theta \]  

(4.4.1)

is satisfied. \( n \) is an integer related to the order of the diffraction, \( \lambda \) is the x-ray wavelength, \( d \) is the perpendicular distance between lattice planes and \( \theta \) is the Bragg’s angle [113]. The XRD measurements were performed on a Philips X-ray diffractometer type PW 1710. A typical sample size for XRD measurement was 0.20 g. This was loaded on a standard sample holder by using a glass slide. The top of the powder was flattened without pressing by the edge of a glass slide. The diffractometer uses a monochromatic beam of CoK\( \alpha \) radiation with an average wavelength 1.7903 Å. The XRD measurements were scanned in the range of 2\( \theta \) from 20° to 80° in steps of 0.01°. The lattice parameters were obtained by refinement of XRD data by a Rietveld analysis (FullProf Suite for Windows). The peak broadening of the most intense 311 peak was used to estimate the crystallite average sizes by the Scherrer formula [114]

\[ D = \frac{K\lambda}{\beta\cos\theta}, \]

(4.4.2)

where \( K \) is a crystal shape factor near unit and \( \beta \) is the full width at half maximum (FWHM) of the peak. We used a \( K \) value of 0.9 ± 0.1 corresponding to nearly spherical crystallites with corundum structure. Figure 4.5 shows a schematic diagram of the mechanical assembly of an Empyrean PAN analytical diffractometer type PW 1710 with CoK\( \alpha \) radiation source operated over a 2\( \theta \) range from 10° to 80°. \( \omega \) is the angle of incidence of the X-rays [115]. The XRD machine used for the current set of measurements is shown in Figure 4.6. Most modern X-ray diffractometers include software for peak profile fitting. This software greatly helps in calculating the intensities, positions, widths, shapes of the peaks and takes into account the broadening of the peaks. To apply the proper correction for the instrumental broadening, the shape of the peak has to be chosen. The two most commonly assumed line shapes are the Lorentzian and
Gaussian [116]. The instrumental broadening was corrected using a Lorentzian line shape in our case.

Figure 4.5: Mechanical assembly of a typical $2\theta$ coupled X-ray diffractometer.

Figure 4.6: PW 1710 Empyrean PANalytical X-ray diffractometer, Geology (WC), UKZN.
4.5 Rietveld refinement details

Rietveld refinement of these compositions were carried out using the XRD data with a Rietveld refinement program FULLPROF [117]. Rietveld refinement has nothing to do with structure determination. To start refining a structure an initial model (even if incomplete) is necessary. This model is supposed to be obtained from a crystal structure solver program or by any other means. Special tutorial documents on Rietveld refinement are included in the distribution of FullProf. The best to start working with FullProf is to edit a previously existent PCR-file and modify it as wished. The background was fitted with 6-Coefficient polynomial function, while the peak shapes were described by pseudo-Voigt profiles. In all the refinements, scale factor, lattice parameters, positional coordinates (x, y, z) and thermal parameters were varied. Occupancy parameters of all the ions were kept fixed during refinement. No correlation between the positional and thermal parameters was observed during refinement and as such it was possible to refine all the parameters together. For more information on how to use the programme, the Commission on Powder Diffraction of the International Union of Crystallography has published some guidelines for Rietveld refinement [117]. The PCR file used in the present work is given Table 4.2.

Table 4.2: PCR file for the as-prepared samples of Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$.

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4.6 Transmission Electron Microscopy

Transmission electron microscopy (TEM) is a technique that uses a beam of electrons transmitted through ultra-thin specimens. An image of the atomic arrangement is formed through the interaction of the transmitted electrons with the specimen. TEM is capable of imaging at a significantly high resolution than light microscopes owing to the small de Broglie wavelengths of the electrons. This enables the instrument’s user to examine fine details even as small as a single column of atoms [118]. TEM forms a major analysis method in a wide range of fields such as biological sciences, material science and nanotechnology. TEM has been extensively used to examine the structure and the crystalline defects such as cracks, dislocations in the compounds such as metals, alloys, ceramics, glasses, polymers, semiconductors and mixtures of these materials [119]. TEM appears in several types of equipment such as high-resolution electron microscopy (HRTEM), scanning transmission electron microscopy (STEM) and atomic electron microscopy (AEM). When extended to HRTEM, information on individual atomic planes or columns of the atoms can be obtained. In TEM, images of the samples can be obtained on suitably prepared thin specimens by appropriate lenses which gather information from very small regions of the sample. The images are formed from the interaction of electrons with the sample. The specimen must be thin enough to transmit electrons and to allow enough intensity of electrons to fall on a fluorescent screen. The maximum resolution of a TEM is limited by the wavelength of the probing source and the aperture of the system. A TEM facility consists of four main components namely an electron optical column, vacuum system, electronics and control software. We have used a type Jeol-JEM 1010 shown in Figure 4.7 to study the microstructure and to estimate the particle sizes of some of our samples. A small sample size of about 0.0002 g was dispersed in ethanol and vibrated in a 80Hz\40 Watt transistorized sonic cleaner for 3 minutes. A copper thin film sample holder with
diameter of about 0.0005 mm is dipped into the dispersed sample and loaded in the equipment in order to produce scanned images of the sample.

Figure 4.7: Joel-JEM-1010 high-resolution transmission electron microscope, EM Unit (WC), UKZN.
4.7 Mössbauer measurements

4.7.1 Experimental set-up

The basic experimental set-up for Mössbauer Spectroscopy consists of several components as shown by the block diagram in Figure 4.8. A suitable radioactive source is used as a spectroscopic tool. This is achieved by changing the energy of the emission spectrum of the source with respect to that of the absorber (specimen) by moving the source towards and away from the absorber. This is equivalent to Doppler shifting the energy of the $\gamma$-rays. This tunes the absorber in and out of resonance making it possible to scan through the different absorption lines and measure the hyperfine interactions. There are different approaches used to measure $\gamma$ rays at different energies (velocities). In a constant velocity Mössbauer spectrometer [104], [120], the transmitted photons through a sample in a fixed time interval are measured at constant velocity. The Mössbauer spectrum is accumulated as constant velocity is changed. In this way the spectrum is scanned stepwise, one velocity at a time. The constant velocity spectrometer consists of $\gamma$ ray detection system, a timer and a scaler for registering accumulated counts at each velocity. Although this is considered to be less expensive than the velocity-sweep experiment, it is tedious to operate unless it is fully automated. Moving the source at constant velocity with high reproducibility and stability while restricted to small amplitude of movement is also not easy to achieve. $^{57}$Fe Mössbauer spectroscopy employed here uses a conventional spectrometer with a $^{57}$Co source sealed in Rh matrix which is vibrated at constant acceleration. The Mössbauer spectrum develops with time as counts are accumulated as a function of the velocity of the source. The Mössbauer spectra were calibrated against a natural iron ($\alpha$-Fe) absorber foil with thickness of about 0.025 mm and purity 99.5%. Isomer shifts are calculated with respect to the $\alpha$-Fe absorber. At least 1 million passes were recorded for one spectrum to be analyzed. The accumulated data at room temperature were interpreted as spectra.
and displayed on the output screen of the computer using MCS-32 software version 2.13 (Ortec). The data were fitted using Recoil Mössbauer analysis software [121].

4.8 Magnetization measurements

4.8.1 Vibrating sample magnetometer

A vibrating sample magnetometer (VSM) is an instrument that is widely used to measure magnetic properties. In Figure 4.9 we show the LakeShore model 735 VSM equipment used in this work [122]. The system consists of a 735 VSM controller and the vibrating head mounted above the Janis helium cryostat. The bottom neck of the cryostat is centered between the pole faces of the electromagnet. Pick-up coils are mounted on the faces of the poles of the electromagnet. Other critical components of the system include a 642 bipolar electromagnet power supply, 340 temperature controller, 450 Gaussmeter, a NESLAB ThermoFlex 2500 chiller and a National Instrument IEEE-488 interface card installed in a desktop computer for data collection. The principle of operation of a VSM is based on Faraday’s law of induction which defines the induced
voltage produced in the pick-up coils that is proportional to the magnetization of the sample. In Faraday’s law

\[
\frac{d\Phi}{dt} = -E
\]  

(4.8.1)

where \(\frac{d\Phi}{dt}\) is the rate of change of magnetic flux and \(E\) is the induced voltage. This induced voltage is proportional to the magnetic moment of a sample and hence its magnetization. A VSM works by detecting the voltage induced by a varying field associated with a vibrating sample. The calibration was done with a standard high-purity (99.995 %) spherical nickel sample of known saturation magnetization \((M_S = 54.7 \text{ emu/g})\) [123]. After the calibration, the sample to be measured was placed in a cylindrical sample holder which is screwed to the lower end of a vibrating sample rod. The rod was gently lowered into the sample space to the final position of the sample between the pick-up coils. The data was collected using the interface card and the data acquisition software installed on the computer [124]. The \(M - H\) curves obtained were then analyzed using Origin software for windows.

Figure 4.9: Lakeshore 735 vibrating sample magnetometer, Condensed Matter Physics Lab (WC), UKZN.
4.8.2 Mini cryogen free system

A mini cryogen free system (CFS)(purchased from Cryogenic Ltd,UK) used in this work consists of a cryo-cooler system, variable temperature insert (VTI), electronics rack, measurement systems software installed on a desktop computer and superconducting magnet. The operating system is similar to that of the VSM for magnetization measurements. However, it has the potential to measure magnetic fields up to 5 tesla with a temperature range of 1.6 K to 700 K. The VTI provides the option of varying the sample temperature. In addition the CFS has inserts for high temperature VSM, AC susceptibility, resistivity and Hall effect measurements. Only the VSM low temperature option was used in the present set of measurements. The calibration for magnetization measurement on this system was done using yttrium iron garnet sphere. Procedures such as evacuating the VTI, helium gas inlet, helium dump, vacuum, and recharging the dump were carried out to avoid possible contamination in the helium dump and sample space by air. The procedures are discussed in manuals. The operation of the system is carried out by software commands using a LabVIEW graphical programming software interface. Only procedures such as disconnection-reconnection of hoses and sample mounting are done manually. Figure 4.10 shows the set up of the mini cryogen-free VTI system used for measurements. The sample preparation and loading is different from that of the LakeShore VSM. A small amount of 0.005 g of sample is required for measurements. The sample was loaded into a Perspex cone and held fixed by cotton wool to avoid torque. The loaded Perspex cone was guided into an 80 mm length of straw through a slit made at a position of about 20 mm on the straw. The position of the sample in the cone was fixed around the 20 mm position which was firmly held together with the straw by a piece of Kapton tape.
Figure 4.10: Mini cryogen-free VTI system, Condensed Matter Physics Lab (WC), UKZN.
The straw was then screwed to the probe rod using the adaptor provided on the rod and mounted into the airlock position shown in Figure 4.11. The lowering of the sample probe into the sample space was prompted by series of commands from the sample load option in the software menu. The sample load option was selected from the menu window. This prompted an automatic series of commands such as flushing the air space with helium gas, setting the sample space up to operating pressure and vibration of the sample rod. After the centring of the sample, the required temperatures and fields for measurements were entered using the edit sequence command from the menu window. Finally the measurements were executed using the execute sequence command. The low temperature magnetizations are performed under field cooling (FC) and zero field cooling (ZFC). For the ZFC magnetization curve, the sample is first cooled in a zero field from room temperature to the lowest temperature. Then a magnetic field is applied and the magnetization can be measured as a function of temperature while warming the sample to room temperature. In FC, the sample is cooled in a field to the lowest temperature. The magnetization curve is obtained in the same field while increasing the temperature of the sample. Three magnetization setups were used in the present work. This was based on available resources during the course of the study.

Figure 4.11: VTI VSM probe attached to a sample, Condensed Matter Physics Lab (WC), UKZN.
Chapter 5

Structure and magnetic properties of Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nano oxides

In this chapter we present work that has been published in the Journal of Magnetism and Magnetic Materials 385 (2015) 282-285. Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nano oxides were produced by hydrothermal process. The following results are presented: (XRD) and TEM measurements confirming the single corundum structure and nanophase structure. The variation of coercive field with particles size reveals that the coercive field achieves a maximum at a critical particle size. These results show evidence of transformation from multi-domain to single-domain structure.

5.1 Introduction

In this chapter, we investigate the structural and magnetic properties of Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ alloys synthesized via hydrothermal route. These alloys are derived from the structure of hematite ($\alpha$-Fe$_2$O$_3$) which has attracted the attention of chemists and physicists alike for many years [22]. The crystal structure is that of corundum ($\alpha$-Al$_2$O$_3$) with a closed-packed oxygen lattice and Fe$^{3+}$ cations in octahedral sites. This alloy is antiferromagnetic below the Morin transition at $T = 250$ K and undergoes a transition above the Morin temperature to a weak ferrimagnetic state as a result of spin cant-
ing, before finally becoming paramagnetic at high temperatures $T \geq 948$ K \cite{18}, \cite{125}.

The introduction of dopants modifies the magnetic properties of the alloy. The dopant metal ions substitute for Fe$^{3+}$ in the corundum-related structure of $\alpha$-Fe$_2$O$_3$ with the consequent formation of cationic and anionic vacancies \cite{48}, \cite{55}. The difference in ionic radii between the dopant metal ion and that for Fe$^{3+}$ will influence the structural characteristics and phase behavior of the doped system. The tin-doped $\alpha$-Fe$_2$O$_3$ alloys have been found to exhibit sensing properties for gases such as methane and carbon monoxide \cite{46, 65}. It is well known that small particle size and large surface area can improve the performance of materials used as sensors or catalysts and that the particle size and surface area are related directly to the preparation method and conditions. Below a critical size the domain structure of the particles changes from multidomain to single domain behavior \cite{126} resulting into interesting magnetic properties \cite{127, 128}.

In general, upon reduction in the size $D$, ferromagnetic materials become magnetically harder and exhibit increased coercivity. However, below a certain size, the coercivity is observed to decrease and soft magnetism begins to prevail. This appears to be a common feature for metal oxides \cite{126, 128, 129} and Fe-based alloys \cite{130}. In Fe-based mechanically alloyed nanocrystalline materials, the coercive field $H_C$ is found to follow a $D^6$ power law relation \cite{130}, while other size dependences of $H_C$ have also been observed in iron oxides \cite{127}, \cite{128}.

Hematite $\alpha$-Fe$_2$O$_3$ has shown potential as a photoanode for water splitting because it possesses several desirable properties \cite{49, 131}. The synthesis and characterisation of tin-doped iron oxides and tin-doped chromium oxides have been reported previously \cite{77, 132, 133}. Although there have been several studies of the $\alpha$-Fe$_{2-x}$Cr$_x$O$_3$ \cite{39, 75, 76} system, there appears to have been little activity in the doping of these materials by tin. Berry et al. \cite{77} have examined the magnetic interactions in tin-doped $\alpha$-Cr$_2$Fe$_x$O$_3$ by $^{57}$Fe and $^{119}$Sn-Mössbauer spectroscopy. Following this work, we present a more detailed account of magnetic interactions in $\text{Sn}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$. We
have investigated how single phase formation is influenced by various factors such as the synthesis method, conditions and route. In this respect, Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nano-materials have been synthesized by hydrothermal reaction in a reflux system and a pressure reactor from pure metal chlorides at about 100 °C. We have also examined the onset of the single domain structure as a function of particle size and how it relates to the observed properties such as coercive fields and magnetization. The reduction in particle size was achieved by milling of the as-prepared samples [9].

### 5.2 Experimental details

Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ alloys with $x$ ranging from 0.3 to 1.3 were produced by the low temperature synthesis based on the hydrothermal process in a stirred pressure reactor (Figure 4.1) and in a reflux system (Figure 4.2) [111]. All the samples were subjected to thermal annealing in air for 12 hours at 600 °C. Three additional samples were produced by milling the sample of composition Sn$_{0.2}$Fe$_{1.5}$Cr$_{0.3}$O$_3$ for 1 hour, 2 hours and 3 hours respectively. The particle size reductions were performed by mechanical milling using a Retsch MP 400 planetary ball mill. Details for the synthesis methods used to produce different samples have been discussed in chapter 4. All samples were characterized by X-ray diffraction (XRD) using CoK\ensuremath{\alpha} radiation with wavelength of 1.7903 Å on a Phillips diffractometer (type: PW1710). A Jeol model JEM-1010 transmission electron microscopy (TEM) was used to obtain the morphology of the samples. The $^{57}$Fe Mössbauer spectra of the as-prepared samples were recorded at about 300 K in zero field using a conventional constant acceleration Mössbauer spectrometer with a $^{57}$Co source sealed in rhodium matrix. A standard natural iron foil was used to calibrate the spectra in terms of the transmitted intensity against velocity of the source. The magnetization measurements at room temperature were performed using a Lakeshore model 735 vibrating sample magnetometer (VSM).
5.3 Results and discussion

5.3.1 X-ray diffraction and transmission electron microscopy measurements

The XRD measurements were scanned in the range \(20^\circ \leq 2\theta \leq 80^\circ\) in steps of 0.01°/s.

The XRD patterns of the as-prepared samples of \(\text{Sn}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3\) with \(0.3 \leq x \leq 1.3\) are shown in Figure 5.1 for samples made in a pressure reactor.

Figure 5.1: XRD patterns recorded for \(\text{Sn}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3\) synthesized in a stirred pressure reactor at 100 °C and 120 psi. The arrows show small impurities.
The patterns recorded from the samples were characteristic of the corundum related structure of these materials despite the presence of small impurities peaks. The XRD patterns were different from those recorded from pure $\alpha$–Fe$_2$O$_3$ and $\alpha$-Cr$_2$O$_3$ [134]. In particular, the relative intensities of the two peaks characterising the (104) and (110) reflections in the region of 33°-36° in 2$\theta$ were reversed. This was strongly suggestive of pronounced preferred orientation in the samples typical of an acicular habit [134], with elongation along $\langle 001 \rangle$ providing an intensity enhancement of the $(h k 0)$ reflections.

The results are similar to those recorded from tin-doped $\alpha$–Fe$_2$O$_3$ [66], $\alpha$-Cr$_2$O$_3$ [133] and tin-doped $\alpha$-(FeCr)$_2$O$_3$ [77]. It appears that in solid solutions of the type $\alpha$–Fe$_x$(Cr$_{1.8-x}$O$_3$) tin occupies similar sites as it does in both $\alpha$–Fe$_2$O$_3$ and $\alpha$-Cr$_2$O$_3$ [20].

The refinement of XRD patterns was then performed by a Rietveld analysis according to an identical model to that was previously used to refine the diffraction data of tin-doped $\alpha$–Fe$_2$O$_3$ [133] and $\alpha$-Cr$_2$O$_3$ [20]. The structure of $\alpha$–Fe$_2$O$_3$ has Fe$^{3+}$ ions distributed in an ordered fashion in 2/3 of the octahedral sites within a framework of hexagonally close-packed O$^{2-}$ ions. Chains of face sharing octahedra are directed along the c axis, and the Fe$^{3+}$ ions within each chain form pairs as shown in Figure 5.2. It is was shown [133] that for such structures, the data cannot be fitted to a simple model in which Sn$^{4+}$ substitute for Fe$^{3+}$ with charge balance being achieved by an appropriate number of cations vacancies. Such a simple model would introduce face-sharing of SnO$_6$ and FeO$_6$ octahedra which would create high cation repulsions.

The model that we use involves tin ions substituting on two of the octahedral Fe$^{3+}$ sites in corundum related $\alpha$-Fe$_2$O$_3$. Elimination of Fe$^{3+}$ cations from the octahedra adjacent to the Sn$^{4+}$ creates two additional octahedral sites that do not involve face sharing and which are therefore amenable to occupation by additional Sn$^{4+}$ ions. The structure is formed by defect clusters comprising a chain of three tin ions which all avoid face-sharing repulsions as shown in Figure 5.3. The cluster is electrically neutral since 4 Fe$^{3+}$ ions are replaced by 3 Sn$^{4+}$ ions. In the final stage of the refinements, the
Figure 5.2: Linking of FeO$_6$ or CrO$_6$ octahedra along $c$ in $\alpha$-Fe$_2$O$_3$ or $\alpha$-Cr$_2$O$_3$.

Figure 5.3: Structural model involving the substitution of 4Fe$^{3+}$ or 4Cr$^{3+}$ ions by 3 Sn$^{4+}$ ions.
cation site occupancies were constrained in accordance with the model. Representative measured data and refinement results for Sn$_{0.2}$Fe$_{0.3}$Cr$_{1.5}$O$_3$ are shown in Figure 5.4, where the black circles indicate the experimental data, red solid line indicates the Rietveld refinement fit by Fullprof analysis software. The green curve at the bottom reveals the difference between the fit and the experimental data. The complete set of final refined parameters are shown in Table 5.1. The structural parameters show little deviation from those of ideal α-Fe$_2$O$_3$ and α-Cr$_2$O$_3$ [134], which suggests that the defect clusters can be incorporated into the corundum structure with very little lattice strain.

Figure 5.5 shows the variations of the XRD patterns of Sn$_{0.2}$Fe$_{x}$Cr$_{1.8-x}$O$_3$ for samples made in a reflux system. The main intensity peaks correspond to reflections from (012), (104), (110), (113), (024), (116), (018), (214) and (300) planes which characterize the
Table 5.1: Refined Structural Parameters for samples made in a pressure reactor.

<table>
<thead>
<tr>
<th>Atom</th>
<th>( x/a )</th>
<th>( y/b )</th>
<th>( z/c )</th>
<th>( U_{iso} \times 100/A^2 )</th>
<th>Occupancy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sn(<em>2)Fe(</em>{0.3})Cr(_{1.5})O(_3)</td>
<td>0.0000</td>
<td>0.0000</td>
<td>0.3463(2)</td>
<td>0.500(0)</td>
<td>9.016(2)</td>
</tr>
<tr>
<td>Fe</td>
<td>0.0000</td>
<td>0.0000</td>
<td>0.3463(2)</td>
<td>0.500(0)</td>
<td>1.696(2)</td>
</tr>
<tr>
<td>Sn1</td>
<td>0.0000</td>
<td>0.0000</td>
<td>0.3463(2)</td>
<td>0.500(0)</td>
<td>0.447(3)</td>
</tr>
<tr>
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<td>0.0000</td>
<td>0.0000</td>
<td>0.000(0)</td>
<td>0.500(0)</td>
</tr>
<tr>
<td>O1</td>
<td>0.3217(1)</td>
<td>0.0000</td>
<td>0.2500(0)</td>
<td>0.500(0)</td>
<td>18.000(0)</td>
</tr>
<tr>
<td>( R_{wp} ) (%)</td>
<td>14.4</td>
<td>( R_{exp} ) (%)</td>
<td>9.5</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Sn(<em>2)Fe(</em>{0.5})Cr(_{1.3})O(_3)</td>
<td>0.0000</td>
<td>0.0000</td>
<td>0.35173(2)</td>
<td>0.500(0)</td>
<td>8.594(2)</td>
</tr>
<tr>
<td>Fe</td>
<td>0.0000</td>
<td>0.0000</td>
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<td>0.500(0)</td>
<td>2.118(2)</td>
</tr>
<tr>
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<td>0.0000</td>
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<td>1.290(3)</td>
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<tr>
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<td>0.0000</td>
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<td>0.500(0)</td>
</tr>
<tr>
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<td>0.3217(1)</td>
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<td>0.2500(0)</td>
<td>0.500(0)</td>
<td>18.000(0)</td>
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<tr>
<td>( R_{wp} ) (%)</td>
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<td>( R_{exp} ) (%)</td>
<td>9.3</td>
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<td></td>
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<td>Sn(<em>2)Fe(</em>{0.9})Cr(_{1.1})O(_3)</td>
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<td>0.500(0)</td>
<td>9.055(0)</td>
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<tr>
<td>Fe</td>
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<td>2.415(0)</td>
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<td>0.270(0)</td>
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<td>0.500(0)</td>
</tr>
<tr>
<td>O1</td>
<td>0.30800(0)</td>
<td>0.0000</td>
<td>0.250(0)</td>
<td>0.500(0)</td>
<td>18.000(0)</td>
</tr>
<tr>
<td>( R_{wp} ) (%)</td>
<td>14.4</td>
<td>( R_{exp} ) (%)</td>
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<td></td>
<td></td>
</tr>
<tr>
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<td>0.0000</td>
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<td>0.500(0)</td>
<td>10.260(0)</td>
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<td>0.500(0)</td>
<td>1.207(0)</td>
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<td>0.34690(0)</td>
<td>0.500(0)</td>
<td>0.269(0)</td>
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<tr>
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<td>0.0000</td>
<td>0.000(0)</td>
<td>0.500(0)</td>
</tr>
<tr>
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<td>0.30800(0)</td>
<td>0.0000</td>
<td>0.250(0)</td>
<td>0.500(0)</td>
<td>18.000(0)</td>
</tr>
<tr>
<td>( R_{wp} ) (%)</td>
<td>13.4</td>
<td>( R_{exp} ) (%)</td>
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<td></td>
<td></td>
</tr>
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<td>1.810(0)</td>
</tr>
<tr>
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<td>0.0000</td>
<td>0.34689(0)</td>
<td>0.500(0)</td>
<td>0.269(0)</td>
</tr>
<tr>
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<td>0.0000</td>
<td>0.0000</td>
<td>0.000(0)</td>
<td>0.500(0)</td>
</tr>
<tr>
<td>O1</td>
<td>0.3217(1)</td>
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<td>0.500(0)</td>
<td>18.000(0)</td>
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<tr>
<td>( R_{wp} ) (%)</td>
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<td>( R_{exp} ) (%)</td>
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<td></td>
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<td>Sn(<em>2)Fe(</em>{1.3})Cr(_{0.5})O(_3)</td>
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<td>0.0000</td>
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<td>0.284(0)</td>
<td>9.178(0)</td>
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<td>0.0000</td>
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<td>2.051(0)</td>
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<tr>
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<td>0.0000</td>
<td>0.000(0)</td>
<td>0.500(2)</td>
</tr>
<tr>
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<td>( R_{wp} ) (%)</td>
<td>14.5</td>
<td>( R_{exp} ) (%)</td>
<td>9.6</td>
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corundum structure as indicated in Figures 5.1 and 5.5. The measured data was refined using Fullprof software against the theoretical parameters from the model used previously [134]. The results indicate very small changes in unit cell size between the samples made in a reflux glass condenser and those made in a pressure reactor. Direct measurement of the particle size and powder morphology for the as-prepared samples were also performed by transmission electron microscopy (TEM). The TEM images in Figure 5.6 show that the samples consist of small nanosized particles. The calculated $D_{XRD}$ and measured $D_{TEM}$ values appear to be in good agreement. The lattice parameters, the average particle diameters as calculated from XRD data ($D_{XRD}$) and observed by TEM measurements ($D_{TEM}$) are shown in Table 5.2.
Table 5.2: Particle size \((D_{XRD})\), \((D_{TEM})\) and lattice parameters for as-prepared Sn\(_{0.2}\)Fe\(_x\)Cr\(_{1.8-x}\)O\(_3\) samples.

<table>
<thead>
<tr>
<th>(x)</th>
<th>Reflux</th>
<th>Pressure reactor</th>
</tr>
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<tbody>
<tr>
<td></td>
<td>(a = b)</td>
<td>(c)</td>
</tr>
<tr>
<td></td>
<td>(Å)</td>
<td>(Å)</td>
</tr>
<tr>
<td>±10(^{-3})</td>
<td>±10(^{-3})</td>
<td>±10(^{-3})</td>
</tr>
<tr>
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<td>4.961</td>
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</tr>
<tr>
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<td>4.990</td>
<td>13.696</td>
</tr>
<tr>
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<td>4.985</td>
<td>13.643</td>
</tr>
<tr>
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<td>4.986</td>
<td>13.635</td>
</tr>
<tr>
<td>0.9</td>
<td>5.024</td>
<td>13.778</td>
</tr>
<tr>
<td>1.3</td>
<td>4.986</td>
<td>13.638</td>
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The errors in \(D_{XRD}\) are calculated using the formula
\[
\delta D_{XRD} = \sqrt{\left(\frac{\Delta K}{K}\right)^2 + \left(\frac{\Delta \lambda}{\lambda}\right)^2 + \left(\frac{\Delta \beta}{\beta}\right)^2 + \left(\frac{\Delta \theta}{\theta}\right)^2} \quad (5.3.1)
\]
based on the Scherrer formula. The shape of the crystallite are not uniform. It is realistic to assume \(\Delta K \simeq \pm 0.1\). This makes a significant contribution to the calculated error in Table 5.2. The volume of the samples do not significantly change despite the incorporation of Fe\(^{3+}\) with smaller ionic radii into the sites of Cr\(^{3+}\) with larger ionic radii. The general trend of \(D\) for the different samples shows similar patterns for the samples made by reflux and in a pressure reactor. The samples made in a pressure reactor appear to have a slightly reduced particle size than those made in a glass reflux system. Considering the uncertainties, except for the sample \(x = 0.9\), the \(D\)-values are similar and there is no difference between samples prepared in reflux and in
pressure reactor. This argument is also supported by the TEM data, which show similar values between the samples. The $D$-values obtained from TEM also agree with those estimated from XRD data, except for samples with $x = 0.9$ and 1.1, but with values in acceptable range discrepancy. T. Nguyen et al. [135] have studied the nucleation and growth of nanoparticles. This theory gives a basic outline of how to control particle formation within solution by elucidating the key controllable parameters: reaction temperature, supersaturation, time and the surface energy which can be controlled indirectly through the choice of surfactants. Each material will nucleate and grow depending on its reaction conditions and even a small change in condition, such as pH, can lead to a completely different mechanisms [136].

Figure 5.6: Variation of particle size with iron content for the as-prepared samples of $\text{Sn}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$. 

\[
\begin{align*}
D_{\text{RD}} & \quad \text{D}_{\text{RD}} \\
D_{\text{TEM}} & \quad \text{D}_{\text{TEM}}
\end{align*}
\]
Figure 5.7: TEM micrographs for the Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples prepared (a) in an open reflux vessel and (b) in pressure reactor.
5.3.2 Mössbauer measurements

The $^{57}$Fe Mössbauer spectra recorded from Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples at 300 K are shown in Figures 5.8 (reflux) and 5.9 (pressure reactor). It can be seen that the spectra of the samples with $x = 0.3$ and $x = 0.5$ are paramagnetic doublets. The spectra for $x = 0.7$ and $x = 0.9$ show paramagnetic component with a non-zero electric field gradient around $^{57}$Fe isotopes. For $x \geq 1.1$ sextets are observed. Each Mössbauer spectrum has been fitted with two magnetic components in the form of two sextets, one sextet and one doublet or two doublets. The sextet with the higher hyperfine field is attributed to Fe$^{3+}$ ions without Cr$^{3+}$ or Sn$^{4+}$ in their neighborhood lattice sites. The second sextet with lower hyperfine field is due to Fe$^{3+}$ ions with Cr$^{3+}$ and Sn$^{4+}$ neighbors. This interpretation of hyperfine fields is similar to the work of Berry et al. [133] in Sn and Ti doped $\alpha$-Fe$_2$O$_3$ samples. The doublets are observed in samples that have higher Cr content. This reflects the collapse of magnetic interaction with increase Cr content associated with more negative exchange interactions leading to doublets. All the components in the spectra recorded at 300 K were characterised by nearly constant chemical isomer shifts of about 0.35(5) mm/s confirming that the accommodation of tin into the corundum-related structure did not induce a change in the Fe$^{3+}$ oxidation state of iron [20]. Insignificant change in isomer shifts indicates that the s-electron density is not much affected by substitution of Cr by Fe atoms. The values of the isomer shifts and the hyperfine fields recorded in Table 5.3 are comparable to those reported for similar compounds [106]. The variation of the component with maximum hyperfine magnetic field with increasing iron content $x$ in spectra recorded at 300 K is shown in Figure 5.10. It appears that the hyperfine field increases as the iron content $x$ increases. The samples produced by reflux show higher magnetic hyperfine fields than the samples made in a pressure reactor. This is due to the fact that the samples made by reflux have particle sizes that are slightly higher at the
same composition than those of samples made in a pressure reactor. This decreasing tendency of the magnetic hyperfine fields at small particle sizes may be due to both the surface effect and the size effect. As the particle size decreases to nanoscale, the volume of the surface atoms is an appreciable fraction of that in the total volume, and both the small-size effect and the surface effect perturb the structure and the properties of the nanoparticles. In ferromagnetic and ferrimagnetic oxides, magnetic coupling is very sensitive to the atomic environment. The smaller the particle size the higher the fraction of surface atoms and the lower the contribution to the total magnetic moment [137].
Figure 5.9: Room temperature $^{57}$Fe Mössbauer spectra recorded for Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples produced via the pressure reactor. The solid lines are the LSQ fits.
Figure 5.10: The variation of the component with maximum hyperfine magnetic field with increasing iron content $x$ for Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$.

Table 5.3: Hyperfine parameters from Mössbauer spectra recorded at room temperature for the as-prepared samples of Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$.

<table>
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<tr>
<th>$T = 300$ K</th>
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<th>doublet 2</th>
<th>sextet 1</th>
<th>sextet 2</th>
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<td>$\delta$</td>
<td>$\Delta$</td>
<td>$f$</td>
<td>$\delta$</td>
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<tr>
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<td>$\pm 0.01$</td>
<td>$\pm 0.02$</td>
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</tr>
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<tr>
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<td>-0.11</td>
<td>465</td>
<td>56</td>
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<tr>
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<td>64</td>
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<table>
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<td>0.35</td>
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<td>0.35</td>
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85
5.3.3 Magnetization measurements

The isothermal magnetization measurements presented here were performed at room temperature using a Lakeshore vibrating sample magnetometer [124]. Hysteresis loops of the samples in powder forms were obtained in an external applied field up to 14 kOe. The magnetization measurements at room temperature obtained from Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples made in a reflux and in a pressure reactor are presented in Figures 5.11 and 5.12 respectively. The results show that the hysteresis loops obtained from the two synthesis methods are similar. The hysteresis loops are symmetric and not shifted with respect to the origin. It worth noting that the hysteresis loops for samples with $x \leq 0.7$ appear to consist of a paramagnetic phase where the $M - H$ plots are linear and have a magnetically ordered phase at low fields associated with hysteresis whilst for $x > 0.7$, the magnetization increases significantly. The samples exhibit nearly zero remanence and zero coercivity suggesting a superparamagnetic behavior for nanocrystalline iron oxides [20]. The magnetization does not appear to saturate even at the maximum applied field. The slow approach to saturation can be explained on the basis of the disordered spin configuration at the surface of the magnetic nanooxides [20]. The samples with lower iron concentration have similar magnetic properties as α-Cr$_2$O$_3$ [71] whilst those with higher iron concentration display properties of α-Fe$_2$O$_3$ [22]. The magnetic properties such as coercivity $H_C$, saturation magnetization $M_S$ and remanance $M_R$ were estimated from the magnetic hysteresis loops. The coercive field is calculated as

$$H_C = \left| \frac{H_1 + H_2}{2} \right|$$  \hspace{1cm} (5.3.2)

where $H_1$ and $H_2$ are fields at the left and right side of the shifted magnetization curves respectively. The remanent magnetization is also obtained from the vertical magnetization shifts. The uncertainties have been found by standard deviation using Origin software. The coercive fields are significantly reduced with increase in Fe content.
Figure 5.11: Hysteresis loops measured at room temperature for Sn_{0.2}Fe_{x}Cr_{1.8-x}O_{3} prepared in a reflux.

Figure 5.12: Hysteresis loops measured at room temperature for Sn_{0.2}Fe_{x}Cr_{1.8-x}O_{3} prepared in a pressure reactor.
while the saturation magnetization increases. The saturation magnetization was taken as the magnetization at the highest applied field. This is a reasonable estimate if we are interested in elucidating the trends in the properties with increasing iron concentration. The coercive field is a measure of the magnetization reversal processes under the action of an applied field. It depends on the domain structure, particle sizes and crystalline anisotropy. The coercive field of Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nanoparticles have been studied as a function of iron content. The substitution by Fe atoms leads to a reduction in $H_C$. In Figures 5.13-5.15 we have plotted the coercive fields, remanent magnetizations and saturation magnetizations as a function of iron content. The data obtained for magnetization measurements are presented in Table 5.3. The results show that the hysteresis disappears as the iron content increases. The magnetization data for $x > 0.7$ display a nearly zero coercive field which could be related to small particles in superparamagnetic state while Mössbauer data show no superparamagnetic state for most of Fe atoms in the prepared materials. This discrepancy may be due to the different time window of these experimental techniques. The saturation magnetization $M_S$ values measured for the samples gradually increases with Fe$^{3+}$ substitution. This may be due to the fact that Cr$^{3+}$ ions (magnetic moment 3 $\mu$B) are replaced by stronger magnetic Fe$^{3+}$ ions (magnetic moment 5 $\mu$B). The ratio $M_R/M_S = S$ is referred to as the squareness of a hysteresis loop [127] where $M_R$ is the remanent magnetization. It is derived to determine whether the intergrain exchange exists or not [138]. Stoner and Wohlfarth have reported $S = 0.5$ for randomly oriented non-interacting particles, while $S < 0.5$, particles interact by magnetostatic interaction [138]. In this series of alloys, all samples $S$ values are less than 0.5 indicating that particles interact by magnetostatic interactions. We have further investigated the effect of the reduction of particle sizes on magnetization by mechanical milling on a Sn$_{0.2}$Fe$_{1.3}$Cr$_{0.5}$O$_3$ sample. The hysteresis curves are shown in Figure 5.16 and the magnified view in Figure 5.17. The various parameters deduced from the hysteresis loops are given in Table 5.4. A significant drop
in magnetization and an increase in coercive field are observed on reducing grain sizes from about 28 nm to 24 nm (after 2 hours of milling). The reduction in magnetization is attributed to weakening of magnetic coupling between moments. The reduction in magnetization can also be explained by structural distortions in the surface of the powders compared to that of bulk compounds [139], [140]. This compares well with the evolution of the superparamagnetic phase in the Mössbauer spectra with decreasing grain size. A slight reduction in coercive field is also observed when the particle size is further reduced to 17 nm (after 3 hours of milling). The coercive field appears to achieve a maximum value of about 207 Oe at a critical sample particle size of about 22.8 nm as shown in Figure 5.18. This trend is expected to be closely related to the change in magnetic hardness of the samples [135]. Similar behavior has been observed elsewhere [19]. This decrease at larger sizes can be explained on the basis of a crossover effect from single-domain to multi-domain behavior at a critical particle size [141]. After about 3 hours of milling no significant change in the particle size occurs

Table 5.4: Coercive fields ($H_C$), saturation magnetizations ($M_S$), remanent magnetizations ($M_R$) and ratio $M_R/M_S$ for Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples.

<table>
<thead>
<tr>
<th>Sample $x$</th>
<th>$H_C$ (Oe)</th>
<th>$M_R$ (emu/g)</th>
<th>$M_S$ (emu/g)</th>
<th>$M_R/M_S$</th>
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<td>Reflux</td>
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<td></td>
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<tr>
<td>0.3</td>
<td>278 ± 4</td>
<td>0.1 ± 0.1</td>
<td>2.0 ± 0.1</td>
<td>0.02</td>
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<tr>
<td>0.5</td>
<td>220 ± 0.5</td>
<td>0.1 ± 0.1</td>
<td>2.1 ± 0.1</td>
<td>0.03</td>
</tr>
<tr>
<td>0.7</td>
<td>210 ± 0.2</td>
<td>0.2 ± 0.1</td>
<td>4.2 ± 0.1</td>
<td>0.03</td>
</tr>
<tr>
<td>0.9</td>
<td>33 ± 0.5</td>
<td>0.5 ± 0.1</td>
<td>10.3 ± 0.1</td>
<td>0.05</td>
</tr>
<tr>
<td>1.1</td>
<td>22 ± 0.8</td>
<td>0.8 ± 0.1</td>
<td>13.2 ± 0.1</td>
<td>0.06</td>
</tr>
<tr>
<td>1.3</td>
<td>18 ± 1.1</td>
<td>1.1 ± 0.1</td>
<td>16.2 ± 0.1</td>
<td>0.07</td>
</tr>
<tr>
<td>Pressure reactor</td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.3</td>
<td>287 ± 0.4</td>
<td>0.1 ± 0.1</td>
<td>2.3 ± 0.1</td>
<td>0.04</td>
</tr>
<tr>
<td>0.5</td>
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<td>0.1 ± 0.1</td>
<td>3.4 ± 0.1</td>
<td>0.03</td>
</tr>
<tr>
<td>0.7</td>
<td>228 ± 0.2</td>
<td>0.2 ± 0.1</td>
<td>4.6 ± 0.1</td>
<td>0.04</td>
</tr>
<tr>
<td>0.9</td>
<td>43 ± 0.4</td>
<td>0.4 ± 0.1</td>
<td>6.9 ± 0.1</td>
<td>0.05</td>
</tr>
<tr>
<td>1.1</td>
<td>31 ± 0.9</td>
<td>0.9 ± 0.1</td>
<td>11.9 ± 0.1</td>
<td>0.07</td>
</tr>
<tr>
<td>1.3</td>
<td>28 ± 1.1</td>
<td>1.1 ± 0.1</td>
<td>13.8 ± 0.1</td>
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</table>
Figure 5.13: Coercive field $H_C$ versus iron concentration for $\text{Sn}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$ samples.

Figure 5.14: Remanent magnetization $M_R$ versus iron concentration ($x$) for the as-prepared $\text{Sn}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$ samples.

with further grinding. For single-domain particles the coercive field can be expected
Figure 5.15: Saturation magnetization $M_S$ versus iron concentration ($x$) for the as-prepared Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples.

to increase with increase in particle size $D$ according to the relation [141]

$$H_C = a_m + b_m/D$$  \hspace{1cm} (5.3.3)

where $a_m$ and $b_m$ are constants. We have plotted $H_C$ versus $1/D$ in Figure 5.19 to test the validity of Eq. (5.3.3) and determined the constants $a_m$ and $b_m$. A good fit to the data (correlation coefficient of 0.9396) has been observed. We obtained the values of $a_m$ and $b_m$ for the Sn$_{0.2}$Fe$_{1.3}$Cr$_{0.5}$O$_3$ oxide to be $-1.1 \pm 0.45$ kOe and $32.5 \pm 11.85$ nm kOe, respectively. The value of $b_m$ might be related to the magnetic coupling between the moments [19]. For multi-domain particles, $H_C$ is expected to decrease with further increase in particle size as [141]

$$H_C = a_s - b_s/D^2.$$  \hspace{1cm} (5.3.4)

A graph of $H_C$ versus $1/D^2$ for the Sn$_{0.2}$Fe$_{1.3}$Cr$_{0.5}$O$_3$ oxide is shown in Figure 5.20. This gives the constant $a_s$ and $b_s$ to be $0.48$ kOe and $-109.29$ (nm)$^2$ kOe (with a correlation coefficient of 0.98057). The coercive field is closely related to processes that limit the

91
Figure 5.16: Room temperature hysteresis loops for the milled Sn$_{0.2}$Fe$_{1.3}$Cr$_{0.5}$O$_3$.

Figure 5.17: Magnified view of hysteresis loops measured at low fields for milled Sn$_{0.2}$Fe$_{1.3}$Cr$_{0.5}$O$_3$. 
Figure 5.18: Coercive field $H_C$ versus particle size $D$ for Sn$_{0.2}$Fe$_{1.3}$Cr$_{0.5}$O$_3$. The solid line is the LSQ fit.

Figure 5.19: Variation of coercive fields for Sn$_{0.2}$Fe$_{1.3}$Cr$_{0.5}$O$_3$ with $1/D$ for $D < 23$ nm below transition point for ball milled samples. The solid line is the LSQ fit.
motion of domain walls in a material. In the present system of compounds we assume that this arises due to an increased number of grain boundaries with milling [130]. The milling process increases the number of multidomain particles. A nonlinear variation in coercivity and anisotropy constant can be explained on the basis of particle size as with the reduction of particle size, the surface to volume ratio increases and surface effects may induce a spin disorder in surface layer which results in enhanced anisotropy [142, 143].

Table 5.5: Effect of the milling time on the nanoparticles properties.

<table>
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<tr>
<th>Sn_{0.2}Fe_{1.3}Cr_{0.5}O_{3}</th>
<th>Milling time (min)</th>
<th>$H_C$ (Oe)</th>
<th>$D$ (nm)</th>
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<tr>
<td></td>
<td>0</td>
<td>±4</td>
<td>±0.02</td>
</tr>
<tr>
<td></td>
<td>60</td>
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<td>28.48</td>
</tr>
<tr>
<td></td>
<td>120</td>
<td>195</td>
<td>26.23</td>
</tr>
<tr>
<td></td>
<td>130</td>
<td>231</td>
<td>24.48</td>
</tr>
<tr>
<td></td>
<td>150</td>
<td>268</td>
<td>22.98</td>
</tr>
<tr>
<td></td>
<td>170</td>
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<tr>
<td></td>
<td>180</td>
<td>185</td>
<td>18.64</td>
</tr>
</tbody>
</table>

Figure 5.20: Variation of coercive fields for Sn_{0.2}Fe_{1.3}Cr_{0.5}O_{3} with $1/D^2$ for $D > 23$ nm. The solid line is the LSQ fit.
5.3.4 Conclusion

Nanoparticles of $\text{Sn}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$ oxides with single phase corundum structure were synthesized directly by the hydrothermal method. There were no significant difference in the particle sizes of the samples made in reflux and in a pressure reactor as determined by XRD and TEM analysis. However, the samples prepared using a pressure reactor appear to be have particle sizes that are slightly smaller. The composition variations also appear to follow similar trends. Evidence of successful Sn incorporation into the corundum structure is obtained [20]. The milled sample of $\text{Sn}_{0.2}\text{Fe}_{1.3}\text{Cr}_{0.5}\text{O}_3$ shows reduced magnetization with reduction in grain size and an associated increase in coercive field after milling for 2 hours. The coercive fields have been found to vary with particle size according to Equations 5.3.3 and 5.3.4 corresponding to single-domain and multi-domain behavior respectively.
Chapter 6

Structure and magnetic properties of Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nano oxides

6.1 Introduction

In this chapter we present the structure and magnetic properties of Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nanosized alloys with $0.3 \leq x \leq 0.9$. The samples were synthesized at low reaction temperature of about 100 °C by using the hydrothermal method in a pressure reactor. We managed to produce samples with particle sizes in the range between 32.8 and 55.6 nm. The structures and magnetic properties of the synthesized samples were investigated on the as-prepared samples annealed at 600 °C and on samples annealed at 700 °C. The evolutions of the properties as a function of composition were investigated by XRD, TEM, Mössbauer spectroscopy, magnetization and susceptibility measurements.

6.2 Experimental details

High-purity metal chlorides were used as starting materials to make 0.1 molar (M) solutions for the hydrothermal process. The synthesis procedures is similar to what we have presented before [20, 21]. Excess aqueous ammonia was slowly added to the chloride mixture until full precipitation. The precipitate was boiled in deionised water in a pressure reactor for 3 hours. The products were then filtered and washed
with deionized water several times until no chloride ions were detected by addition of drops of silver nitrate standard solution. The clean products were finally washed with ethanol and then dried under an infrared 250 W lamp. The resulting homogeneous powders were heated in air at 600 °C for 12 hours. The X-ray diffraction (XRD) patterns of the samples were obtained by using CoKα radiation (λ = 1.7903 Å) on a Philips diffractometer (type: PW 1710). The Mössbauer spectra were recorded at about 300 K using a conventional constant acceleration spectrometer with a $^{57}$Co source sealed in Rh matrix. Magnetization measurements were obtained by using a Quantum Design vibrating sample magnetometer operated between 10 K and 400 K [21]. These measurements included hysteresis loops, zero field cooling (ZFC) and field cooling (FC) magnetizations.

### 6.3 Results and discussion

#### 6.3.1 X-ray diffraction

Figure 6.1 shows the XRD patterns for the Mg$_{0.2}$Fe$_2$Cr$_{1.8-x}$O$_3$ alloys. The patterns confirm the formation of the basic corundum structure in all samples. These XRD results are similar to those of Sn doped α-Fe$_2$O$_3$ [66, 133]. No impurity phases were observed in the patterns. The refinement of XRD data was performed by Rietveld analysis (FullProfSuite for Windows) using a model involving a combination of both interstitial and substitutional Mg$^{2+}$ ions in octahedral coordination [134]. The structure of α-Fe$_2$O$_3$ has Fe$^{3+}$ ions distributed in an ordered fashion in 2/3 of the octahedral sites within a framework of hexagonally close-packed O$^{2-}$ ions. Chains of face sharing octahedra are directed along the c axis, and the Fe$^{3+}$ ions within each chain form pairs as shown in Figure 6.2. All refinements in which the oxygen occupancy was allowed to vary implied no vacancies on the oxygen sublattice and provided strong evidence of the validity of the model illustrated in Figure 6.3 [77]. The lower charge on magnesium ion
allows the formation of a linear defect cluster of three \( \text{Mg}^{2+} \) species. In the final stage of the refinements, the cation site occupancies were constrained in accordance with the model described above as shown in Table 6.1. The average grain sizes were obtained using the Debye-Scherrer equation (4.4.2) [114]. Direct measurement of the crystal lite sizes and powder morphology of the as-prepared samples were also performed by transmission electron microscopy (TEM). The TEM pictures are shown in Figures 6.4 and 6.5.

Figure 6.1: XRD patterns recorded for \( \text{Mg}_{0.2} \text{Fe}_x \text{Cr}_{1.8-x} \text{O}_3 \) samples.
Figure 6.2: Linking of FeO$_6$ or CrO$_6$ octahedra along $c$ in $\alpha$-Fe$_2$O$_3$ or $\alpha$-Cr$_2$O$_3$.

Figure 6.3: Structural model involving the substitution of 2Fe$^{3+}$ or 2Cr$^{3+}$ ions by 3Mg$^{2+}$ ions.
Table 6.1: Refined Structural Parameters for Mg\textsubscript{0.2}Fe\textsubscript{x}Cr\textsubscript{1.8—x}O\textsubscript{3} samples.

<table>
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<tr>
<th>Atom</th>
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<th>(y/b)</th>
<th>(z/c)</th>
<th>(U_{iso} \times 100/A^2)</th>
<th>Occupancy</th>
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<td>(R_{exp} (%))</td>
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<td>10.5</td>
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\(\text{Mg}_{0.2}\text{Fe}_{0.3}\text{Cr}_{1.5}\text{O}_3\)

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\(\text{Mg}_{0.2}\text{Fe}_{0.5}\text{Cr}_{1.3}\text{O}_3\)

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\(\text{Mg}_{0.2}\text{Fe}_{0.7}\text{Cr}_{1.1}\text{O}_3\)

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\(\text{Mg}_{0.2}\text{Fe}_{0.9}\text{Cr}_{0.9}\text{O}_3\)
Figure 6.4: TEM micrographs for $\text{Mg}_{0.2}\text{Fe}_{0.3}\text{Cr}_{1.5}\text{O}_3$ and $\text{Mg}_{0.2}\text{Fe}_{0.5}\text{Cr}_{1.3}\text{O}_3$ samples.
Figure 6.5: TEM micrographs for Mg$_{0.2}$Fe$_{0.7}$Cr$_{1.1}$O$_3$ and Mg$_{0.2}$Fe$_{0.9}$Cr$_{0.9}$O$_3$ samples.
The shapes of the particles appear to be nearly spherical with a significant spread in the particle sizes for all the alloys studied. Hence, the mean square estimation of the diameters has been used to calculate the average grain size $D_{TEM}$ from at least 30 particles on each micrograph. The lattice parameters, the average particle diameters as calculated from XRD data ($D_{XRD}$) and observed by TEM measurements ($D_{TEM}$) are shown in Table 6.2. The calculated $D_{XRD}$ and measured $D_{TEM}$ values of the particle sizes are in good agreement. The particle sizes appear to be sensitive to Cr concentration for $x = 0.3$, $0.5$ and $0.9$ where a reduction in particle sizes is observed with increase in Fe content except for the $x = 0.7$ alloy which has an unusually high particle size. This alloy appears more relaxed with slightly higher unit cell volume which we assume to be more likely due to longer synthesis or sintering time.

Table 6.2: Particle sizes ($D_{XRD}$), ($D_{TEM}$) and lattice parameters for as-prepared $\text{Mg}_0.2\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$ samples.

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<th>$a = b$ (Å)</th>
<th>$c$ (Å)</th>
<th>$V$ (Å$^3$)</th>
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<th>$D_{TEM}$ (nm)</th>
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<td>53 ±2</td>
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<td>4.985 ±10$^{-3}$</td>
<td>13.643 ±10$^{-3}$</td>
<td>294.34 ±10$^{-3}$</td>
<td>42.5 ±0.8</td>
<td>41 ±2</td>
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<td>0.7</td>
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<td>13.622 ±10$^{-3}$</td>
<td>296.23 ±10$^{-3}$</td>
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<td>13.586 ±10$^{-3}$</td>
<td>291.4 ±10$^{-3}$</td>
<td>32.8 ±0.8</td>
<td>37 ±2</td>
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</table>
6.3.2 Mössbauer measurements

The variation of Mössbauer spectra as a function of $x$ for the $\text{Mg}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$ recorded at room temperature is shown in Figure 6.6. It can been seen that the spectra of the samples with $x = 0.3$ and $x = 0.5$ are paramagnetic doublets. The spectra for $x = 0.7$ and $0.9$ show paramagnetic component with a non-zero electric field gradient around $^{57}\text{Fe}$ isotopes. The spectra for alloys with low Fe concentration ($x \leq 0.5$) were best fitted to two doublets. The doublets are associated with Fe ions in paramagnetic spin states. For $x = 0.7$ and $0.9$, the spectra show the superposition of a sextet pattern and a broad doublet. In this case the spectra could be fitted to a single sextet and a doublet patterns.

Figure 6.6: Room temperature $^{57}\text{Fe}$ Mössbauer spectra recorded for $\text{Mg}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$ samples. The solid lines are the LSQ fits.
The solid lines are the result of fittings to the experimental data and correspond to individual components (sextets or doublets). There was no significant change in isomer shifts and quadrupole splitting with increasing $x$. A slight increase in hyperfine fields from 442 kOe to 469 kOe has been observed for the fitting sextet. This is due to an increase in Fe content, a behavior that can increase $T_N$. The $^{57}$Fe Mössbauer spectra showed no evidence for the oxidation of Fe$^{3+}$ to Fe$^{2+}$ as result of the incorporation of Mg$^{2+}$. This is therefore consistent with charge balance not involving a change in the oxidation state of iron. The Mössbauer fit parameters are presented in Table 6.3.

Table 6.3: Hyperfine parameters from Mössbauer spectra recorded at room temperature for the as-prepared samples of Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$. The solid line is the LSQ fits.

<table>
<thead>
<tr>
<th>Sample</th>
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<th>Doublet 2</th>
<th>Sextet 1</th>
<th>Sextet 2</th>
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<tbody>
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<td></td>
<td></td>
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</tr>
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<td></td>
<td>$\delta$</td>
<td>$\Delta f$</td>
<td>$\delta$</td>
<td>$\Delta f$</td>
<td>$2\varepsilon$</td>
</tr>
<tr>
<td></td>
<td>mm/s</td>
<td>mm/s</td>
<td>%</td>
<td>mm/s</td>
<td>mm/s</td>
</tr>
<tr>
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<td>± 0.01</td>
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<td>± 0.01</td>
<td>± 0.02</td>
<td>± 0.01</td>
</tr>
<tr>
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<td>0.35</td>
<td>0.9</td>
<td>29</td>
<td>0.36</td>
<td>0.39</td>
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<td>0.7</td>
<td>0.33</td>
<td>0.52</td>
<td>59</td>
<td>0.29</td>
<td>1.11</td>
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<td>0.9</td>
<td>0.37</td>
<td>1.07</td>
<td>25</td>
<td>0.36</td>
<td>-0.11</td>
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<td>0.9</td>
<td>0.32</td>
<td>0.67</td>
<td>17</td>
<td>0.37</td>
<td>-0.11</td>
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### 6.3.3 Magnetization measurements

The magnetic properties of the Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nanooxides were also determined. The temperature variation of the magnetization for the as-prepared samples measured after zero field cooling (ZFC) and field cooling (FC) regimes are shown in Figures 6.7-6.10. The lower curve for each sample in all Figures correspond to ZFC and the upper curve to FC. During FC, the samples were cooled from 400 K to 10 K in the presence of an external magnetic field of 50 Oe. For ZFC measurements, the samples were cooled to 10 K in zero field. The magnetizations were recorded during warming up to 400 K in the presence of the same external field. The magnetization for the FC curve decreases
continuously with increasing temperature. With decreasing temperature both ZFC and FC magnetizations rise and separate at a temperature ($T_G$) where it is assumed that the ferromagnetic (FM) clusters begin to form [144] due to short range coupling of magnetic moments. At a lower temperature $T_B$ called the blocking or freezing temperature the ZFC magnetizations reach a maximum where the moments of the FM clusters begin to freeze. The blocking temperature depends on the average particle size [128]. As expected $T_B$ increases with increased particle size for all samples except for the $x = 0.7$ sample. The width of the peak in ZFC curve is associated with particle size distribution. A narrow peak observed in ZFC curve for $x = 0.9$ indicates narrow distribution of particle sizes. A bifurcation between the FC and ZFC curves usually implies the existence of a cluster-glass [144, 145] and is possibly due to the magnetic frustration induced by the surface-driven spin frustration and disorder in the nanoparticles [146], [147, 148]. These results indicate cluster-glass-like behavior. According to equation (2.4.36) and as shown in Figure 2.3, the linear fits for the temperature dependence of the inverse magnetization show that the samples exhibit Curie-Weiss type behavior above 286 K and 290 K for $x = 0.7$ and $x = 0.9$ respectively. The corresponding extrapolated paramagnetic Weiss temperatures $\theta_p$ are -354 K and -722 K. The corresponding effective magnetic moments are 3.83 $\mu_{eff}$ and 4.23 $\mu_{eff}$. The theoretical value can be obtained as follows: $\mu_{eff} = (0.2 \times 5.92 + 0.9 \times 3.87)\mu_B = 4.67 \mu_B$. The experimental values are slightly smaller than the theoretical value. Figure 6.11 shows typical results for $x = 0.9$. The large negative values of $\theta_p$ indicate that the antiferromagnetic (AFM) interactions in Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ are strong. Figures 6.12 to 6.15 show the field dependencies of the magnetization for different compositions in the alloys series Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ recorded at 400 K. The inset of these figures show the amplified hysteresis loop.
Figure 6.7: Temperature dependence of ZFC and FC magnetizations of the as-prepared Mg$_{0.2}$Fe$_{0.3}$Cr$_{1.5}$O$_3$ sample.

Figure 6.8: Temperature dependence of ZFC and FC magnetizations of the as-prepared Mg$_{0.2}$Fe$_{0.5}$Cr$_{1.3}$O$_3$ sample.
Figure 6.9: Temperature dependence of ZFC and FC magnetizations of the as-prepared \( \text{Mg}_{0.2}\text{Fe}_{0.7}\text{Cr}_{1.1}\text{O}_3 \) sample.

Figure 6.10: Temperature dependence of ZFC and FC magnetizations of the as-prepared \( \text{Mg}_{0.2}\text{Fe}_{0.9}\text{Cr}_{0.9}\text{O}_3 \) sample.
An anomalous variation of magnetization with low magnetic field is observed. This behavior might have application in magnetic switching devices. For purely paramagnetic phases, the magnetization curves at 400 K should be straight lines across the first and third quadrants in the hysteresis loops. However, the plots show that in addition to a paramagnetic phase there is a small magnetic phase in all samples at 400 K. The paramagnetic phase is consistent with doublets in the Mössbauer spectra obtained at 300 K. The magnetic phase appears to grow with an increase in the Fe content of the alloys as indicated by increased hysteresis. We assume that at low temperature, the small magnetic phase evolves into FM clusters which eventually freeze at the blocking temperature while the dominant paramagnetic phase evolves into AFM phase below its corresponding Néel temperature ($T_N$). An increase in coercivity was observed from 400 K to 10 K. The measurements of hysteresis loops at 10 K shown in Figure 6.16-6.19 were performed after field cooling (FC) and zero field cooling (ZFC) measurements. The hysteresis loops are not symmetrical about the origin but are slightly shifted to
Figure 6.12: Magnetization curves of the Mg$_{0.2}$Fe$_{0.5}$Cr$_{1.3}$O$_3$ sample measured at 400 K. The inset shows the amplified hysteresis loop.

Figure 6.13: Magnetization curves of the Mg$_{0.2}$Fe$_{0.5}$Cr$_{1.3}$O$_3$ sample measured at 400 K. The inset shows the amplified hysteresis loop.
Figure 6.14: Magnetization curves of the Mg$_{0.2}$Fe$_{0.7}$Cr$_{1.1}$O$_3$ sample measured at 400 K. The inset shows the amplified hysteresis loop.

Figure 6.15: Magnetization curves of the Mg$_{0.2}$Fe$_{0.9}$Cr$_{0.9}$O$_3$ sample measured at 400 K. The inset shows the amplified hysteresis loop.
Figure 6.16: Magnetization curves of the Mg$_{0.2}$Fe$_{0.3}$Cr$_{1.5}$O$_3$ sample measured at 10 K. The inset shows the amplified hysteresis loop.

Figure 6.17: Magnetization curves of the Mg$_{0.2}$Fe$_{0.5}$Cr$_{1.3}$O$_3$ sample measured at 10 K. The inset shows the amplified hysteresis loop.
Figure 6.18: Magnetization curves of the Mg$_{0.2}$Fe$_{0.7}$Cr$_{1.1}$O$_3$ sample measured at 10 K. The inset shows the amplified hysteresis loop.

Figure 6.19: Magnetization curves of the Mg$_{0.2}$Fe$_{0.9}$Cr$_{0.9}$O$_3$ sample measured at 10 K. The inset shows the amplified hysteresis loop.
the left side. The shift of the hysteresis loop along the field axis is associated with exchange bias effects [149]. The direct exchange interaction between ferromagnetic and anti-ferromagnetic spins in a common interface results in unidirectional magnetic anisotropy seen as exchange bias effect. The theory of exchange bias effect was discussed in Chapter 2. In the present case for Mg$_{0.2}$Cr$_{1.8-x}$Fe$_x$O$_3$ nanoparticle alloys, the exchange bias is due to the exchange interaction between the antiferromagnetic (AFM) and ferromagnetic (FM) spin clusters dominated by Cr and Fe atoms respectively. The exchange bias phenomenon has applications in magneto-electronic switching devices, random access magnetic storage units, magnetic sensors and spintronics devices [150]. The exchange bias field is defined as

$$H_{EB} = \left| \frac{H_{C1} - H_{C2}}{2} \right|$$

where $H_{C1}$ and $H_{C2}$ are coercive fields at the left and right side of the shifted magnetization curves respectively [150]. The values of the exchange bias field $H_{EB}$ deduced from hysteresis loops measured at 10 K are shown in Table 6.3, which we can correlate with iron content $x$ and particle sizes presented in Table 6.1. In Figure 6.20 we observe that there is no correlation between $H_{EB}$ and iron content $x$. Figure 6.21 shows the particle size dependence of $H_{EB}$ for all our samples. The exchange bias field $H_{EB}$ seems to correlate very well with the particle sizes $D$. This is consistent with previous studies which show larger bias at larger particle sizes [150, 151]. The presence of AFM domains in this case is expected to account for the particle size dependence of $H_{EB}$ by an argument similar to AFM layer thickness dependence of FM-AFM films [151]. The correlation in Figure 6.21 is also interesting because it suggests a critical particle size of about 31 nm when $H_{EB}$ is zero for this series of alloys.
Table 6.4: Values of exchange bias fields for as-prepared Mg\textsubscript{0.2}Fe\textsubscript{x}Cr\textsubscript{1.8–x}O\textsubscript{3} samples annealed at 600 °C.

<table>
<thead>
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<th>x</th>
<th>$H_{EB}$ (Oe)</th>
<th>$D_{XRD}$ (nm)</th>
</tr>
</thead>
<tbody>
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<td>± 0.5</td>
<td>± 0.04</td>
</tr>
<tr>
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<td>135.0</td>
<td>55.61</td>
</tr>
<tr>
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<td>64.1</td>
<td>42.32</td>
</tr>
<tr>
<td>0.7</td>
<td>192.3</td>
<td>65.91</td>
</tr>
<tr>
<td>0.9</td>
<td>10.2</td>
<td>32.83</td>
</tr>
</tbody>
</table>

Figure 6.20: Iron content dependence of exchange bias field $H_{EB}$ for the Mg\textsubscript{0.2}Fe\textsubscript{x}Cr\textsubscript{1.8–x}O\textsubscript{3} samples measured at 10 K.
Figure 6.21: Particle size dependence of exchange bias field $H_{EB}$ for the Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples measured at 10 K. The solid line is the linear fit to the data with a correlation coefficient of 0.999.

### 6.3.4 Conclusion

We have successfully prepared Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nanoparticle alloys by hydrothermal process. An anomalous variation of magnetization in low fields has been observed. Our results from 400 K to 10 K show evidence of strong antiferromagnetic (AFM) interactions in the alloys. The results also show the presence of weak ferromagnetic (FM) clusters. The nanoparticle oxides have been found to exhibit exchange bias effects which appear to be sensitive to particle sizes. Samples with larger grains show more enhanced exchange bias effect. A strong linear relationship between the exchange bias field ($H_{EB}$) and particles sizes ($D$) has been observed for particle sizes between 32 and 66 nm.
Chapter 7

Effect of annealing on exchange bias in Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nano oxides

7.1 Introduction

Exchange bias is a phenomenon associated with induced exchange anisotropy at the interface between ferromagnetic (FM) and antiferromagnetic (AFM) phases in a heterogeneous system [98]. The exchange bias considerably increases the total anisotropy of the system, which has technological applications for magnetic storage, spin-electron devices and the development of permanent magnets [149]. The exchange bias is observed as the unidirectional shift of a hysteresis loop when a system is cooled down to low temperatures in an external applied magnetic field below the Néel temperature of the AFM phase. In addition to the exchange bias at the FM/AFM interface, exchange bias has also been reported for different systems which involve glassy magnetic behaviour such as FM/spin-glass (SG) bilayer films, core-shell structure and intrinsically phase separated cluster-glass (CG) alloys [152–155]. In most cases, the exchange bias has been investigated on artificially fabricated heterogeneous systems consisting of FM/AFM or FM/SG bilayers or core-shell structures. A fundamental understanding of the nature of intrinsic phase separation of the alloys is therefore important for technological applications. Nieebieskikwiat et al. [156] and Qian et al. [157] have
reported strong effect of exchange bias in the case of charge ordered manganites such as Pr$_{1/3}$Ca$_{2/3}$MnO$_3$ and Y$_{0.2}$Ca$_{0.8}$MnO$_3$. The exchange bias is also reported for cluster-glass cobaltites La(Ba, Sr)CoO$_3$, where the exchange bias is due to the cluster-glass consisting of FM and SG phases [154], [155]. Recently we observed the exchange bias phenomenon in Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ annealed at 600 °C for 12 hours [158]. In this chapter we extend the results presented in chapter 6 and we investigate the effect of further annealing the Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nanoparticles on the exchange bias effect.

7.2 Experimental details

High-purity metal chlorides were used as starting materials to make 0.1 molar (M) solutions for synthesis of Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nano oxides by hydrothermal reaction. The synthesis procedure is similar to what we have presented before [20, 21]. The resulting homogeneous powders were heated in air at 700 °C for 12 hours. The X-ray diffraction (XRD) patterns of the samples were obtained by using CoKα radiation ($\lambda = 1.7903$ Å) on a Philips diffractometer (type: PW 1710). The magnetization measurements were performed using two different systems, namely a Lakeshore model 735 vibrating sample magnetometer (VSM) for room temperature measurements and a Mini cryogen free system for magnetization measurements in applied magnetic fields of up to 50 kOe in the temperature range of 2 - 300 K.

7.3 Results and discussion

7.3.1 X-ray diffraction

Figure 7.1 shows the XRD patterns for the Mg$_{0.2}$Cr$_{1.8-x}$Fe$_x$O$_3$ alloys annealed at 700 °C. The patterns confirm the persistence of the basic corundum structure in all the samples. These XRD results are similar to those of Sn doped $\alpha$-Fe$_2$O$_3$ presented in Chapter
and which were interpreted in terms of tin occupying both octahedral, interstitial and substitutional sites. The average particle sizes were obtained using the Debye-Scherrer equation (4.4.2) [114] and are recorded in Table 7.1.

Figure 7.1: XRD patterns for Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples annealed at 700 °C.
Table 7.1: Particle size ($D_{XRD}$) for Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples.

<table>
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<tr>
<th>$x$</th>
<th>$D_{XRD}$ (nm) ± 0.8</th>
</tr>
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<td>56.45</td>
</tr>
<tr>
<td>0.5</td>
<td>44.01</td>
</tr>
<tr>
<td>0.7</td>
<td>66.55</td>
</tr>
<tr>
<td>0.9</td>
<td>34.01</td>
</tr>
</tbody>
</table>

7.3.2 Magnetization measurements

The magnetic properties of the Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nano oxides annealed at 700 °C were also determined. Figures 7.2 to 7.5 show the field dependencies of the magnetization for different compositions in the alloys series Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ recorded at 300 K. The results show that the hysteresis loops for samples with $x \leq 0.5$ appear to consist of a paramagnetic phase where the $M - H$ plots are almost linear. For samples with $x > 0.5$ there is an additional small magnetically ordered phase in low fields associated with hysteresis. The samples exhibit nearly zero remanence and zero coercivity suggesting a superparamagnetic behavior of the nanocrystalline iron oxides [20]. The magnetic phase appears to grow with increase in the Fe content of the alloys as indicated by increased hysteresis. We observe that at low temperature, the small magnetic phase evolves into FM clusters which eventually freeze at a blocking temperature while the dominant paramagnetic phase evolves into AFM phase below its corresponding Néel temperature ($T_N$). The hysteresis loops recorded at different temperatures are shown in Figures 7.6 - 7.9. It is worth noting that in the $M - H$ curves, the magnetization
Figure 7.2: Hysteresis loop measured for Mg$_{0.2}$Fe$_{0.3}$Cr$_{1.5}$O$_3$ sample.

Figure 7.3: Hysteresis loop measured for Mg$_{0.2}$Fe$_{0.5}$Cr$_{1.3}$O$_3$ sample.
Figure 7.4: Hysteresis loop measured for Mg$_{0.2}$Fe$_{0.7}$Cr$_{1.1}$O$_3$ sample.

Figure 7.5: Hysteresis loop measured for Mg$_{0.2}$Fe$_{0.9}$Cr$_{0.9}$O$_3$ sample.
value increases and does not reach saturation even at the highest magnetic field. This can indicate the dominant role of the AFM components. Thus the Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ may be considered to be composed of AFM cores and FM cluster-glass-like shells. As the temperature is lowered, the finite-range ferromagnetic ordering is constructed in the shell, and the FM clusters form and begin to freeze around the freezing temperature ($T_f$). At low temperature, the samples become magnetically harder due to spin-freezing. The coercive fields increase with decreasing temperature. The coercive field is defined as

$$H_C = \frac{|H_{C1}| + |H_{C2}|}{2},$$  \hspace{1cm} (7.3.1)

where $|H_{C1}|$ and $|H_{C2}|$ relate to the left and right shifts of the hysteresis loops respectively [159]. The raw data for the coercive fields are recorded in Table 7.2 and the temperature dependence of the coercive field $H_C$ obtained from hysteresis loops in the temperature range 2 to 100 K for the Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples studied are shown in Figures 7.10 - 7.13. The temperature dependence of $H_C$ follows well the formula

$$H_C = H_C(0) \exp(-T/T_1),$$  \hspace{1cm} (7.3.2)

where $H_C(0)$ is the extrapolated coercive field at absolute zero temperature and $T_1$ is a constant [159]. The coercive field data is fitted over the entire temperature range with $T_1 = 59.2 \pm 0.1$ K, 143.4 $\pm$ 0.2 K, 30.1 $\pm$ 0.1 K and 18.1 $\pm$ 0.3 K for $x = 0.3$, 0.5, 0.7 and 0.9 respectively.

Table 7.2: Values of coercive fields for Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples annealed at 700 °C.

<table>
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<th>$H_C$ (Oe) ± 0.5</th>
<th>$H_C$ (Oe) ± 0.5</th>
<th>$H_C$ (Oe) ± 0.5</th>
<th>$H_C$ (Oe) ± 0.5</th>
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<td>161.2</td>
<td>112.3</td>
<td>156.1</td>
</tr>
<tr>
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</tr>
<tr>
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<td>100</td>
<td>67.2</td>
<td>37.2</td>
<td>17.1</td>
<td>37.2</td>
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</table>

123
Figure 7.6: Hysteresis loops measured at different temperatures for $\text{Mg}_{0.2}\text{Fe}_{0.3}\text{Cr}_{1.5}\text{O}_3$ sample.
Figure 7.7: Hysteresis loops measured at different temperatures for Mg$_{0.2}$Fe$_{0.5}$Cr$_{1.3}$O$_3$ sample.
Figure 7.8: Hysteresis loops measured at different temperatures for $\text{Mg}_{0.2}\text{Fe}_{0.7}\text{Cr}_{1.1}\text{O}_3$ sample.
Figure 7.9: Hysteresis loops measured at different temperatures for Mg$_{0.2}$Fe$_{0.9}$Cr$_{0.9}$O$_3$ sample.
Figure 7.10: Temperature dependence of the coercive field for the as-annealed sample of \(\text{Mg}_{0.2}\text{Fe}_{0.3}\text{Cr}_{1.5}\text{O}_3\), fitted by exponential functions.

Figure 7.11: Temperature dependence of the coercive field for the as-annealed sample of \(\text{Mg}_{0.2}\text{Fe}_{0.5}\text{Cr}_{1.3}\text{O}_3\), fitted by exponential functions.
Figure 7.12: Temperature dependence of the coercive field for the as-annealed sample of Mg$_{0.2}$Fe$_{0.7}$Cr$_{1.1}$O$_3$, fitted by exponential functions.

Figure 7.13: Temperature dependence of the coercive field for the as-annealed sample of Mg$_{0.2}$Fe$_{0.9}$Cr$_{0.9}$O$_3$, fitted by exponential functions.
Here again, we find that the hysteresis loops are shifted along the magnetic field axis, indicating the presence of exchange bias effects in the samples [149] in the temperature range between 2 and 20 K. The presence of the microscopic unidirectional exchange anisotropy interaction at the FM/AFM interface appears to be responsible for the exchange bias phenomena [151]. In order to verify whether the observed exchange bias like properties are associated with magnetic ordering, we studied the temperature dependence of the exchange bias. In these measurements, the samples were field-cooled to the measuring temperature in an applied field of 50 Oe. Once the measuring temperature was reached, the magnetization loops were measured between ± 50 kOe. The exchange bias fields deduced from the hysteresis loops at different temperatures are given in Table 7.3 and plotted as a function of temperature in Figure 7.14.

Significant exchange bias is observed at low temperatures for the samples annealed at 700 °C. In the core/shell nanoparticle model, the core spin particles are expected to align while the shell spin particles are in randomized states due to the broken exchange bonds at the surfaces of the nanoparticles [98]. This allows the shell to freeze into random directions at the lowest temperatures. The exchange bias decreases with increase in temperature. The AFM order also diminishes due to thermal fluctuations which result in the weakening of interfacial interactions that causes reduction of loop shifts along the field direction. When the temperature approaches $T_N$, $H_{EB}$ vanishes due to the disappearance of AFM order. It should be noted that though exchange bias

Table 7.3: Values of exchange bias fields for Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples annealed at 700 °C.

<table>
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<tr>
<th>$T$ (K)</th>
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<th>$x$</th>
<th>$H_{EB}$ (Oe)</th>
<th>$H_{EB}$ (Oe)</th>
<th>$H_{EB}$ (Oe)</th>
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</tbody>
</table>
has been observed in some bulk materials, including several Heusler alloys, the effect is in most cases limited to low temperatures [151, 157]. In order to further investigate the correlation between the exchange bias and the particle sizes observed in chapter 6, we have measured hysteresis loops at 2 K, 4 K, 10 K and 20 K. Figure 7.15 shows the particle size dependence of $H_{EB}$ for all our samples at the first three temperatures. Contrary to what was observed in Chapter 6, the exchange bias field $H_{EB}$ increases with decreasing particle size $D$, reaches the maximum around 44 nm for $x = 0.5$ and then decreases until it reaches a critical value of about 33 nm when $H_{EB}$ is zero. For the Mg$_{0.2}$Fe$_{x}$Cr$_{1.8-x}$O$_3$ nano oxides, as the particle size decreases, more and more surface spins deviate from the AFM arrangement which implies the increasing proportion of the uncompensated spin shell and the reduction in the AFM core in the nano oxide [157]. At the same time the uncompensated surface spins favor the FM coupling, leading to the increase in FM clusters with reducing particle size. Thus, $H_{EB}$ increases first and reaches its maximum, then decreases with decreasing particle size. Huang et al. [151] have reported similar results of $H_{EB}$ measured at 5 K for La$_{0.25}$Co$_{0.75}$MnO$_3$ nanoparticles with $D<100$ nm.
Figure 7.15: Particle size dependence of exchange bias field $H_{EB}$ measured at $T_m$ for Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples annealed at $T_A$.

**7.3.3 Conclusion**

Nanoparticles of Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ oxides with single phase corundum structure were synthesized directly by the hydrothermal method. A summary of the effects of annealing temperature $T_A$ on the exchange bias effect are shown in Figure 7.15. As expected thermal annealing increases the particle sizes. The sample at $x = 0.5$ shows enhancement of $H_{EB}$ after annealing while reduction of $H_{EB}$ are observed for other samples. As observed in Figure 6.21 a strong correlation was observed between $H_{EB}$ and $D_{XRD}$. After annealing only the sample at $x = 0.5$ introduces an extra data point that correlates with previous results measured at the same temperature $T_m = 10$ K. Our results show exponential temperature dependence of coercive field. Similar temperature dependences have been observed in other alloys such as La$_{1-x}$CaMnO$_3$ [151, 159] and Fe-rich Fe$_x$Zr$_{1-x}$ amorphous alloys [160]. However, there is still no conclusive evidence of the origin of such a temperature dependence. Coercive fields are related to the ease of inducing magnetization reversals due to the effects of pinning of magnetic domain
walls. One possible explanation of the exponential temperature dependence of $H_C$ can involve a decrease in the volume fraction of AFM components with increase in temperature [151].
Chapter 8

Structure and magnetic properties of Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nano oxides

8.1 Introduction

In this chapter we present the structure and magnetic properties of Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nanosized alloys with $x$ ranging from 0.3 to 1.3. The samples were synthesized at low reaction temperature of about 100 °C by using the hydrothermal method using a model 4843 stirred pressure reactor. We have managed to produce samples with particle sizes in the range between 14.2 and 32.8 nm. The structures and magnetic properties of the synthesized samples were investigated on the as-prepared samples annealed at 600 °C. The evolution of the properties as a function of composition was investigated by XRD, TEM, Mössbauer spectroscopy, magnetization and susceptibility measurements.

8.2 Experimental details

High-purity metal chlorides were used as starting materials to make 0.1 molar (M) solutions for hydrothermal reaction. The synthesis procedure is similar to what we have presented before [20, 21]. Excess aqueous ammonia was slowly added to the stoichiometric chloride metal mixture until full precipitation. The precipitate was boiled under pressure in a reactor for 3 hours. The products were then filtered and washed
with deionized water over a Whatman micro-fibre filter (GF/F) several times until no chloride ions were detected by addition of drops of silver nitrate standard solution. The clean products were finally washed with ethanol and then dried under an infrared lamp. The resulting homogeneous powders were heated in air at 600 °C for 12 hours. The X-ray diffraction (XRD) patterns of the samples were obtained by using CoKα radiation (λ = 1.7903 Å) on a Philips diffractometer (type: PW 1710). The Mössbauer spectra were recorded at about 300 K using a conventional constant acceleration spectrometer with a 57Co source sealed in Rh matrix. The magnetization measurements were performed using two different systems, namely a Lakeshore model 735 vibrating sample magnetometer (VSM) for room temperature measurements and a Quantum Design MPMS SQUID magnetometer for magnetization measurements in applied magnetic fields of up 50 kOe in the temperature range of 2 K to 400 K. These measurements included hysteresis loops, zero field cooling (ZFC) and field cooling (FC) magnetizations.

8.3 Results and discussion

8.3.1 X-ray diffraction

Figure 8.1 shows the XRD patterns for the Mn_{0.2}Fe_{x}Cr_{1.8-\_x}O_{3} alloys. The patterns confirm the formation of the basic corundum structure in all samples. Small impurities were observed in the patterns around 45°. These XRD results are similar to those of Sn doped α-Fe_{2}O_{3} presented in Chapter 5 [66], [133] and which were interpreted in terms of tin occupying both octahedral interstitial and substitutional sites. It appears that in solid solutions of the type α-(FeCr)$_2$O$_3$ the manganese ion also occupies similar sites as does tin and magnesium. The refinement of XRD data was performed by Rietveld analysis (FullProfSuite for Windows) using a model involving a combination of both interstitial and substitutional Mn$^{2+}$ ions in octahedral coordination [134].
complete set of final refined parameters are shown in Table 8.1. The average particle sizes were obtained using the Debye-Scherrer equation (4.2) [114]. Direct measurements of the particle sizes and powder morphology for the as-prepared samples were also performed by transmission electron microscope (TEM). The TEM pictures in Figure 8.2 show the presence of small particles. The lattice parameters, the average particle size as calculated from XRD data ($D_{XRD}$) and observed by TEM measurements ($D_{TEM}$) are recorded in Table 8.1. The general trend of $D$ in Figure 8.3 for the different samples shows that the calculated $D_{XRD}$ and measured $D_{TEM}$ values of the particle sizes are in good agreement.

![XRD patterns](image)

Figure 8.1: XRD patterns recorded for the as-prepared $\text{Mn}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$ samples. The arrows indicate small impurities.
Table 8.1: Refined Structural Parameters for Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples.

<table>
<thead>
<tr>
<th>Atom</th>
<th>$x/a$</th>
<th>$y/b$</th>
<th>$z/c$</th>
<th>$U_{iso} \times 100/\text{Å}^2$</th>
<th>Occupancy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cr1</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.34690(0)</td>
<td>0.500(0)</td>
<td>10.260(0)</td>
</tr>
<tr>
<td>Fe</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.34690(0)</td>
<td>0.500(0)</td>
<td>1.207(0)</td>
</tr>
<tr>
<td>Mn1</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.34690(0)</td>
<td>0.500(0)</td>
<td>0.270(0)</td>
</tr>
<tr>
<td>Mn2</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.000(0)</td>
<td>0.500(0)</td>
</tr>
<tr>
<td>O1</td>
<td>0.30800(0)</td>
<td>0.00000</td>
<td>0.2500(0)</td>
<td>0.500(0)</td>
<td>18.000(0)</td>
</tr>
</tbody>
</table>

| Mn$_{0.2}$Fe$_{0.5}$Cr$_{1.3}$O$_3$ |
| Cr1    | 0.00000| 0.00000| 0.34690(0)| 0.500(0)                        | 9.055(0)  |
| Fe     | 0.00000| 0.00000| 0.34690(0)| 0.500(0)                        | 2.415(0)  |
| Mn1    | 0.00000| 0.00000| 0.34690(0)| 0.500(0)                        | 0.500(0)  |
| Mn2    | 0.00000| 0.00000| 0.00000   | 0.000(0)                        | 0.500(0)  |
| O1     | 0.3217(1)| 0.00000| 0.250(0)  | 0.500(0)                        | 18.000(2) |

| Mn$_{0.2}$Fe$_{0.7}$Cr$_{1.1}$O$_3$ |
| Cr1    | 0.00000| 0.00000| 0.34689(0)| 0.500(0)                        | 10.260(0) |
| Fe     | 0.00000| 0.00000| 0.34689(0)| 0.500(0)                        | 1.207(0)  |
| Mn1    | 0.00000| 0.00000| 0.34689(0)| 0.500(0)                        | 0.270(0)  |
| Mn2    | 0.00000| 0.00000| 0.00000   | 0.000(0)                        | 0.500(0)  |
| O1     | 0.30800(0)| 0.00000| 0.2500(0)| 0.500(0)                        | 18.000(0) |

| Mn$_{0.2}$Fe$_{0.9}$Cr$_{0.9}$O$_3$ |
| Cr1    | 0.00000| 0.00000| 0.34689(0)| 0.500(0)                        | 10.260(0) |
| Fe     | 0.00000| 0.00000| 0.34689(0)| 0.500(0)                        | 1.207(0)  |
| Mn1    | 0.00000| 0.00000| 0.34689(0)| 0.500(0)                        | 0.270(0)  |
| Mn2    | 0.00000| 0.00000| 0.00000   | 0.000(0)                        | 0.500(0)  |
| O1     | 0.3217(1)| 0.00000| 0.250(0)  | 0.500(0)                        | 18.000(0) |

$R_{wp}$ (%) 13.4  $R_{exp}$ (%) 10.5

| Mn$_{0.2}$Fe$_{1.1}$Cr$_{0.7}$O$_3$ |
| Cr1    | 0.00000| 0.00000| 0.34689(0)| 0.500(0)                        | 9.658(0)  |
| Fe     | 0.00000| 0.00000| 0.34689(0)| 0.500(0)                        | 1.810(0)  |
| Mn1    | 0.00000| 0.00000| 0.34689(0)| 0.500(0)                        | 0.269(0)  |
| Mn2    | 0.00000| 0.00000| 0.00000   | 0.000(0)                        | 0.500(0)  |
| O1     | 0.3217(1)| 0.00000| 0.250(0)  | 0.500(0)                        | 18.000(0) |

$R_{wp}$ (%) 12.4  $R_{exp}$ (%) 7.5

| Mn$_{0.2}$Fe$_{1.3}$Cr$_{0.5}$O$_3$ |
| Cr1    | 0.00000| 0.00000| 0.34689(0)| 0.500(0)                        | 9.658(0)  |
| Fe     | 0.00000| 0.00000| 0.34689(0)| 0.500(0)                        | 1.810(0)  |
| Mn1    | 0.00000| 0.00000| 0.34689(0)| 0.500(0)                        | 0.269(0)  |
| Mn2    | 0.00000| 0.00000| 0.00000   | 0.000(0)                        | 0.500(0)  |
| O1     | 0.3217(1)| 0.00000| 0.250(0)  | 0.500(0)                        | 18.000(0) |

$R_{wp}$ (%) 12.4  $R_{exp}$ (%) 7.5
Figure 8.2: TEM micrographs for the as-prepared Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples.
Table 8.2: Particle size ($D_{XRD}$) and lattice parameters for Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples.

<table>
<thead>
<tr>
<th>$x$</th>
<th>$a = b$ (Å) ±10$^{-3}$</th>
<th>$c$ (Å) ±10$^{-3}$</th>
<th>$V$ ($Å^3$) ±10$^{-3}$</th>
<th>$D_{XRD}$ (nm) ±0.6</th>
<th>$D_{TEM}$ (nm) ±2</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.3</td>
<td>4.989</td>
<td>13.699</td>
<td>290.40</td>
<td>32.8</td>
<td>31</td>
</tr>
<tr>
<td>0.5</td>
<td>4.986</td>
<td>13.632</td>
<td>288.76</td>
<td>28.9</td>
<td>27</td>
</tr>
<tr>
<td>0.7</td>
<td>5.004</td>
<td>13.646</td>
<td>287.34</td>
<td>26.8</td>
<td>26</td>
</tr>
<tr>
<td>0.9</td>
<td>4.976</td>
<td>13.608</td>
<td>286.53</td>
<td>17.5</td>
<td>18</td>
</tr>
<tr>
<td>1.1</td>
<td>4.989</td>
<td>13.778</td>
<td>283.32</td>
<td>15.3</td>
<td>15</td>
</tr>
<tr>
<td>1.3</td>
<td>5.024</td>
<td>13.768</td>
<td>283.12</td>
<td>14.20</td>
<td>14</td>
</tr>
</tbody>
</table>

Figure 8.3: Variation of particle size with iron content for the as-prepared samples of Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$. 
8.3.2 Mössbauer measurements

The $^{57}$Fe Mössbauer spectra recorded for Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples at 300 K are shown in Figure 8.4. It can been seen that the spectra for $x = 0.3$ and $x = 0.5$ are paramagnetic doublets and were best fitted to two doublets. The spectrum for $x = 0.7$ shows a doublet with a weak sextet pattern, and for $x \geq 0.9$ sextets are being formed. The spectra for Fe content $x = 0.7$, 0.9 and 0.11 were best fitted to one doublet and one sextet while the spectra recorded for $x = 1.3$ were best fitted by the superposition of two sextets. The component with a larger hyperfine magnetic field can be associated with the Fe$^{3+}$ ions without Mn$^{2+}$ ions in nearby lattice sites whereas the component with lower hyperfine magnetic field reflects the lower spin density at Fe$^{3+}$ in the vicinity of Mn$^{2+}$ nearest cation neighbors. The solid lines are the fits to the experimental data and correspond to individual components (sextets or doublets). The doublet was required in the fits of the samples $x = 0.3$ and 0.5 which we associate with Fe ions in the paramagnetic states. The Mössbauer spectra of $x = 0.7$ and 0.9 have been fitted with two magnetic components in the form of one sextet and one doublet while the spectra of $x = 1.1$ and 1.3 were fitted with two sextets. The sextet with the higher hyperfine field is attributed to Fe$^{3+}$ ions without Cr$^{3+}$ or Mn$^{2+}$ in their neighborhood lattice sites. The second sextet with lower hyperfine field is due to Fe$^{3+}$ ions with Cr$^{3+}$ and Mn$^{4+}$ neighbors. This interpretation of hyperfine fields is similar to the work of Berry et al [133] in Sn and Ti doped α-Fe$_2$O$_3$ samples. The doublets are observed in samples that have higher Cr content. This reflects the collapse of magnetic interaction with increase Cr content associated with more negative exchange interactions leading to doublets. All the components in the spectra recorded at 300 K were characterized by a nearly constant chemical isomer shift of 0.32(3) mm/s confirming that the accommodation of manganese into the corundum-related structure did not induce a change in the Fe$^{3+}$ oxidation state [110]. Insignificant change in isomer shifts indicates that the s-electron
density is not much affected by substitution of Cr by Fe atoms or by thermal relaxation of the lattice. The Mössbauer parameter fits are presented in Table 8.2. The results confirm that manganese can also be accommodated in the corundum-related structure without inducing a change in the Fe$^{3+}$ oxidation state as demonstrated before for tin-doped samples [20].

Figure 8.4: Room temperature $^{57}$Fe Mössbauer spectra for the as-prepared Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples. The solids lines are LSQ fits.
Table 8.3: Hyperfine parameters from Mössbauer spectra recorded at room temperature for the as-prepared samples of \( \text{Mn}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3 \). The solid line is the LSQ fits.

<table>
<thead>
<tr>
<th>Sample ( x )</th>
<th>( \delta ) mm/s</th>
<th>( \Delta ) mm/s</th>
<th>( f ) %</th>
<th>( \delta ) mm/s</th>
<th>( \Delta ) mm/s</th>
<th>( f ) %</th>
<th>( 2\varepsilon ) mm/s</th>
<th>( H ) kOe</th>
<th>( f ) %</th>
<th>( 2\varepsilon ) mm/s</th>
<th>( H ) kOe</th>
<th>( f ) %</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.3</td>
<td>0.36</td>
<td>0.38</td>
<td>70</td>
<td>0.33</td>
<td>1.07</td>
<td>30</td>
<td>0.33</td>
<td>1.07</td>
<td>30</td>
<td>0.33</td>
<td>1.07</td>
<td>30</td>
</tr>
<tr>
<td>0.5</td>
<td>0.31</td>
<td>1.08</td>
<td>39</td>
<td>0.37</td>
<td>0.49</td>
<td>61</td>
<td>0.37</td>
<td>0.49</td>
<td>61</td>
<td>0.37</td>
<td>0.49</td>
<td>61</td>
</tr>
<tr>
<td>0.7</td>
<td>0.34</td>
<td>0.9</td>
<td>32</td>
<td>0.37</td>
<td>0.49</td>
<td>61</td>
<td>0.37</td>
<td>0.49</td>
<td>61</td>
<td>0.37</td>
<td>0.49</td>
<td>61</td>
</tr>
<tr>
<td>0.9</td>
<td>0.32</td>
<td>0.37</td>
<td>32</td>
<td>0.37</td>
<td>0.49</td>
<td>61</td>
<td>0.37</td>
<td>0.49</td>
<td>61</td>
<td>0.37</td>
<td>0.49</td>
<td>61</td>
</tr>
<tr>
<td>1.1</td>
<td>0.32</td>
<td>-0.12</td>
<td>432</td>
<td>0.34</td>
<td>-0.09</td>
<td>404</td>
<td>0.34</td>
<td>-0.09</td>
<td>404</td>
<td>0.34</td>
<td>-0.09</td>
<td>404</td>
</tr>
<tr>
<td>1.3</td>
<td>0.35</td>
<td>-0.14</td>
<td>491</td>
<td>0.37</td>
<td>-0.12</td>
<td>494</td>
<td>0.37</td>
<td>-0.12</td>
<td>494</td>
<td>0.37</td>
<td>-0.12</td>
<td>494</td>
</tr>
</tbody>
</table>

8.3.3 Magnetization measurements

Field cooling (FC) and zero field cooling (ZFC) magnetizations as a function of temperature for samples with \( x = 0.7, 0.9, 1.1, 1.3 \) are shown in Figures 8.5 - 8.8. The lower curve for each sample corresponds to ZFC and the upper curve to FC. In ZFC, a sample is cooled in zero field from room temperature to the lowest temperature at about 10 K where a measuring field is applied. The sample is cooled and the magnetization recorded in the same measuring field for FC. The magnetization measurements were performed with increasing temperature from 10 K to about 400 K in an external magnetic field of 50 Oe. The magnetization for the FC curves decrease continuously with increasing temperature. ZFC and FC magnetizations coincide at a spin freezing temperature which depends on the applied field. ZFC magnetization curves increase gradually with increasing temperature and reach maximum values at blocking temperatures. The width of the peak in the ZFC curve is associated with particle size distribution [161]. The slow decrease of the magnetization with further increase in temperature is associated with disordering of particle spins. One of the characteristic features of the plots in Figures 8.5 - 8.8 are reduced magnetizations at lower temperature for ZFC samples. Similar behaviour of FC and ZFC magnetizations have been
Figure 8.5: Temperature dependence of ZFC and FC magnetizations for the as-prepared \(\text{Mn}_{0.2}\text{Fe}_{0.7}\text{Cr}_{1.1}\text{O}_3\).

Figure 8.6: Temperature dependence of ZFC and FC magnetizations for the as-prepared \(\text{Mn}_{0.2}\text{Fe}_{0.9}\text{Cr}_{0.9}\text{O}_3\).
Figure 8.7: Temperature dependence of ZFC and FC magnetizations for the as-prepared Mn$_{0.2}$Fe$_{1.1}$Cr$_{0.7}$O$_3$.

Figure 8.8: Temperature dependence of ZFC and FC magnetizations for the as-prepared Mn$_{0.2}$Fe$_{1.3}$Cr$_{0.5}$O$_3$. 

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considered to be spin-glass like behavior [162]. The ZFC curve for \( x = 0.9 \) shows a maximum in the magnetization at 82 K. Beyond this the magnetization reduces up to about 180 K before it further increases, touching the FC magnetization curve at about 330 K. This type of a double peak structure has been observed elsewhere [163] and was attributed to the bimodal distribution in particle size. At a lower temperature \( T_B \) called the blocking temperature, the ZFC magnetization reaches a maximum where the moments of the FM clusters begin to freeze. The blocking temperature depends on the average particle size [128, 144]. Figure 8.9 shows the linear fit to the temperature dependence of the inverse magnetization for \( x = 0.9 \). This sample clearly exhibits a Curie-Weiss type behavior above 200 K as indicated by the linear fit. The slope of the graph is 0.2 that gives a Curie constant \( C = 5 \). The value of the effective magnetization is found using the formula: \( \mu_{\text{eff}} = 2.84\, C^{1/2} = 6.35\, \mu_B \). The value obtained is lower compared to the theoretical value which is 9.95 \( \mu_B \). This can be explained by the fact that in fitting the curve, we only considered the part that is linear. The corresponding

extrapolated paramagnetic Weiss temperature \( \theta_p \) is -175 K.

The value of \( \theta_p \) shows that the antiferromagnetic interactions (AFM) are weaker in \( \text{Mn}_{0.2}\text{Fe}_{0.9}\text{Cr}_{0.9}\text{O}_3 \) compared to \( \text{Mg}_{0.2}\text{Fe}_{0.9}\text{Cr}_{0.9}\text{O}_3 \) where \( \theta_p \) was -722 K [20].
The isothermal magnetization measurements presented here were performed at room temperature on a Lakeshore vibrating sample magnetometer [124]. Hysteresis loops of the samples in powder forms were obtained in an external applied field of up to ±14 kOe. The magnetization measurements at room temperature obtained from Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples are presented in Figure 8.10. We find lower magnetizations compared to what was observed in Chapter 5 for Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples. The hysteresis loops for all samples appear to consist of a paramagnetic phase where the $M$-$H$ plots are linear and a magnetically ordered phase at low fields associated with hysteresis. The magnetization increases rapidly in fields up to about 3 kOe and then vary almost linearly without reaching any saturation to a field of 14 kOe. This typical weak magnetic response confirms the antiferromagnetic interactions in the samples. This is similar to the main antiferromagnetic interactions in hematite particles responsible of a large magnetic susceptibility in high fields which is superimposed on a spontaneous ferromagnetic moment, coming either from weak ferromagnetism for temperatures above the Morin transition, or from uncompensated moments mainly at the surface of the particles [146]. Evidence of displacement of hysteresis loops are also observed in Figure 8.10. Assymmetric magnetic hysteresis loops exhibiting shifts both in the field and magnetization axis as well as an enhanced coercive field are observed which indicate the existence of exchange bias phenomenon. The vertical and horizontal loop shifts features are due to minor loop effect which means effects that appear when the FC loops are recorded without reaching saturation magnetization regime. The exchange bias effect can be explained on the basis of a phenomenological core-shell model where the core shows AFM behavior and the surrounding shell possesses a net magnetic moment due to a large number of uncompensated surface spins [98, 164]. The variation of the exchange bias $H_{EB}$ with particle size $D$ and iron content $x$ are displayed in Figure 8.11 and Figure 8.12. The values of the exchange bias fields are recorded in Table 8.3.
The exchange bias field increases as the particle size decreases with increased Fe content $x$. The loops shifts are different with different particle sizes suggesting that the materials at room temperature may be superparamagnetic. Strong correlations are also observed between the exchange bias $H_{EB}$ with particle size $D$ (Figure 8.11) and with Fe content $x$ (Figure 8.12). The linear correlation between $H_{EB}$ and $D$ is particularly interesting. It suggests a collapse of $H_{EB}$ to zero at a particle size of about 33 nm. This is a similar value as for the $H_{EB}$ versus $D$ curve for Mg-doped samples [21] for hysteresis loops at 10 K. The main difference in this case is that $H_{EB}$ decreases with increase in $D$. In order to investigate the phenomenon of exchange bias further, we measured isothermal magnetization loops at different temperatures. In Figure 8.13 we present the hysteresis loops for the as-prepared Mn$_{0.2}$Fe$_{1.3}$Cr$_{0.8}$O$_3$ sample measured at 2, 10, 30, 50, 100, 150 and 200 K in applied magnetic fields of up to 50 kOe using a Mini cryogen free magnetization measurement system (Figure 4.9). We observe that the exchange bias decreases at lower temperatures. This is in contrast to what was observed in Chapter 6 for Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nanoparticles and in other literature reports relating to Ni/NiO particles with an average particle size below 30 nm which demonstrated an asymmetrical magnetic hysteresis loop only at low temperatures [165].

The exchange bias field increases as the particle size decreases with increased Fe content $x$. The loops shifts are different with different particle sizes suggesting that the materials at room temperature may be superparamagnetic. Strong correlations are also observed between the exchange bias $H_{EB}$ with particle size $D$ (Figure 8.11) and with Fe content $x$ (Figure 8.12). The linear correlation between $H_{EB}$ and $D$ is particularly interesting. It suggests a collapse of $H_{EB}$ to zero at a particle size of about 33 nm. This is a similar value as for the $H_{EB}$ versus $D$ curve for Mg-doped samples [21] for hysteresis loops at 10 K. The main difference in this case is that $H_{EB}$ decreases with increase in $D$. In order to investigate the phenomenon of exchange bias further, we measured isothermal magnetization loops at different temperatures. In Figure 8.13 we present the hysteresis loops for the as-prepared Mn$_{0.2}$Fe$_{1.3}$Cr$_{0.8}$O$_3$ sample measured at 2, 10, 30, 50, 100, 150 and 200 K in applied magnetic fields of up to 50 kOe using a Mini cryogen free magnetization measurement system (Figure 4.9). We observe that the exchange bias decreases at lower temperatures. This is in contrast to what was observed in Chapter 6 for Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ nanoparticles and in other literature reports relating to Ni/NiO particles with an average particle size below 30 nm which demonstrated an asymmetrical magnetic hysteresis loop only at low temperatures [165].
Figure 8.10: (a) Hysteresis loops measured at room temperature for Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ in a reflux. (b) Magnified view of hysteresis loops at low fields.
Figure 8.11: Particle size dependence of exchange bias field $H_{EB}$ for the as-prepared $\text{Mn}_{0.2}\text{Cr}_{1.8-x}\text{Fe}_x\text{O}_3$ samples measured at room temperature. The red line is the linear fit.

Figure 8.12: Iron content dependence of exchange bias field $H_{EB}$ for the as-prepared $\text{Mn}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$ samples measured at room temperature. The red line is the linear fit.
The shift observed may suggest the existence of spin-glass configurations. In magnetic oxide nanoparticles [146, 166], such configurations possess different structure and magnetic order between the surface and the interior of the nanoparticles. In this case the disfigurement and small cavities of nanoparticles which cause surface spin disorder or canting may be expected to be responsible for the loop shift of the superparamagnetic nanomaterials. The temperature dependence of the exchange bias for the $\text{Mn}_{0.2}\text{Fe}_{1.3}\text{Cr}_{0.5}\text{O}_3$ sample is shown in Figure 8.14. Hysteresis loops of the as-prepared samples of $\text{Mn}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$ with $x = 0.7, 0.9, 1.1$ and $1.3$ recorded at $2 \text{ K}$ are shown in Figures 8.15 - 8.20.

![Hysteresis loops](image)

Figure 8.13: Hysteresis loops for the as-prepared sample of $\text{Mn}_{0.2}\text{Fe}_{1.3}\text{Cr}_{0.5}\text{O}_3$ recorded at different isothermal temperatures.
Figure 8.14: Temperature dependence of the exchange bias field for the as-prepared sample of Mn$_{0.2}$Fe$_{1.3}$Cr$_{0.5}$O$_3$.

Figure 8.15: Hysteresis loops of Mn$_{0.2}$Fe$_{0.3}$Cr$_{1.5}$O$_3$ measured at 2 K.
Figure 8.16: Hysteresis loops of Mn$_{0.2}$Fe$_{0.5}$Cr$_{1.3}$O$_3$ measured at 2 K.

Figure 8.17: Hysteresis loops of Mn$_{0.2}$Fe$_{0.7}$Cr$_{1.1}$O$_3$ measured at 2 K.
Figure 8.18: Hysteresis loops of Mn$_{0.2}$Fe$_{0.9}$Cr$_{0.9}$O$_3$ measured at 2 K.

Figure 8.19: Hysteresis loops of Mn$_{0.2}$Fe$_{1.1}$Cr$_{0.7}$O$_3$ measured at 2 K.
There is no more shift in the hysteresis loop for Mn$_{0.2}$Fe$_{1.3}$Cr$_{0.5}$O$_3$ in Figure 8.20. This implies that there is no more interaction between the AFM host and the ferromagnetic clusters compared to Figures 8.18 or 8.19.

### 8.3.4 Conclusion

We successfully prepared Mn$_{0.2}$Fe$_{x}$Cr$_{1.8-x}$O$_3$ nanoparticle alloys by hydrothermal process. We found much reduced magnetizations for the Mn-based samples compared to Sn-based samples. The composition dependence of the hysteresis loops is not very significant for Mn-based samples. Evidence of successful Mn incorporation into the corundum structure is obtained [20]. The nanoparticle oxides have been found to exhibit exchange bias effects at room temperature which disappear at low temperatures. Strong linear correlation between the exchange bias field $H_{EB}$ with Fe content and particle sizes have been observed. The $H_{EB}$ in the present case disappears at the particle
size of about 34 nm. The exchange bias in the present case arises from the exchange interaction between the AFM host and ferrimagnetic clusters. Mn$^{2+}$ ions which occupy both interstitial and substitutional sites establish ferrimagnetic clusters inside an AFM background. The present findings of exchange bias at room temperature in Mn$_{0.2}$Cr$_{1.8-x}$Fe$_x$O$_3$ samples is interesting and unexpected. The AFM component appears to be more significant at room temperature and less important in the present series of alloys at lower temperature. However, these results are still under investigation in order to provide additional results and explanation.
Chapter 9

Final conclusions and future work

We have investigated the synthesis, structural and magnetic properties of nanosized Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$, Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$, Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ alloys using X-ray diffraction (XRD), Mössbauer spectroscopy and magnetization measurements. The alloys studied were produced by hydrothermal methods in a reflux vessel and in a pressure reactor. In all samples prepared by hydrothermal process, single phase corundum structure formation as indicated by XRD was incomplete at the initial synthesis temperature of 100 °C and was complete after annealing at 600 °C. In addition, we reduced the size of the Sn$_{0.2}$Fe$_{1.3}$Cr$_{0.5}$O$_3$ alloy using high-energy ball milling. Significant reductions in magnetization and changes in coercive fields when particle sizes are reduced from about 28 nm to about 17 nm are induced by mechanical milling. The results show transformation from multidomain to single domain structure at a critical size of about 23 nm [158]. The particle sizes of the as-prepared alloys were found between 25.3 and 34.8 nm in Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$, 38.8 and 55.6 nm in Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ and 14.2 and 32.8 nm in Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$. The particle sizes appear to be sensitive to a particular composition. The magnetic properties derived from magnetization and Mössbauer spectroscopy measurements are sensitive to the microstructure and the doping atoms. The accomodation of tin, magnesium and manganese into the corundum-related structure did not induce a change in the Fe$^{3+}$ oxidation state of iron.
In the Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ alloys, we find that the general trend for particle sizes for different samples are similar. However, the samples made in a pressure reactor appear to have slightly reduced particle sizes than those made in a glass reflux system. The differences can be attributed to the preparation method. In a pressure reactor, the samples are more homogeneously mixed because stirring continues while the mixtures are heated under pressure. The ability of the samples to form bigger particles seems to be affected by continuous stirring. We also suspect that closer proximity of the reacting ions is achieved in a pressure reactor. The differences in particle size in the two methods is also reflected in the magnetic hyperfine fields. We observe that the samples made in a reflux vessel show higher magnetic hyperfine fields than the samples made in a pressure reactor. These decreasing tendencies of the magnetic hyperfine fields at smaller particle sizes may be due to both the surface effect and the size effect. As the particle size decreases to nanoscale, the volume of the surface atoms is expected to be an appreciable fraction of the total volume and both the small-size effect and the surface effect would perturb the structure and the properties of the nanoparticles [167].

The magnetization curves of Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ with low coercive fields are indicative of the onset of superparamagnetic like-behaviour.

Low temperature measurements in the Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ alloys show evidence of spin freezing as confirmed by zero-field cooling (ZFC) and field cooling (FC) magnetizations measurements. Spin freezing at low temperature appears to be associated with increased magnetic hardness. The linear fits for the temperature dependence of the inverse magnetization show that the samples exhibit Curie-Weiss type behavior. The corresponding extrapolated paramagnetic Weiss temperatures $\theta_p$ are -722 K. The large negative values of $\theta_p$ indicate that the antiferromagnetic (AFM) interactions in Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ alloys are stronger. Furthermore, shifts of the hysteresis loops along the field axis associated with exchange bias effects [149] are observed at low temperature in Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples. The exchange bias in the present case arises from
exchange interaction between the AFM host and ferrimagnetic clusters. There is no correlation between the exchange bias $H_{EB}$ and the iron content $x$ while a strong correlation between $H_{EB}$ and particle size $D$ independent of composition for all samples annealed at 600 °C is observed [21].

After annealing at 700 °C we find significant changes between $H_{EB}$ and $D_{XRD}$. At first, the $H_{EB}$ increases with decreasing particle size from 66.55 nm ($x = 0.7$) to 44.01 nm ($x = 0.5$) then decreases with further reduction in particle size. However, we still find very strong correlation for samples at $x = 0.5, 0.3$ and 0.7 [168].

In contrast with what has been observed in the Mg$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ alloys, the Mn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ alloys exhibit exchange bias at room temperature. In this case there is a strong decreasing correlation between the exchange bias and particle sizes. The exchange bias seems also to correlate very well with iron content $x$ [169]. Magnetization measurements show positive exchange interaction with increasing iron content in tin samples while the magnesium and manganese samples collapse the magnetic order.

Our investigations have provided us with useful information on the synthesis, structural, and magnetic properties of nano oxides [20], [21]. Future work can involve the study of Sn$_{0.2}$Fe$_x$Cr$_{1.8-x}$O$_3$ samples not measured at low temperature, the chemical disorder by Mössbauer technique and the investigation of the exchange bias phenomenon by magnetoresistance measurements [170].
Bibliography


[92] E. Manova, B. Kunev, D. Paneva, I. Mitov, L. Petrov, C. Estournès, C. D’Orléan, J. L. Rehspringer, and M. Kurmoo. Mechanochemical synthesis and character-


[119] *http://cnx.org/content/m22963/1.5/*.


[158] K. Mbela, T. Moyo, and J.Z. Msomi. Magnetic studies of Sn$_{0.2}$Cr$_{1.8-x}$Fe$_{x}$O$_{3}$ compounds prepared via the hydrothermal route. *Journal of Magnetism and Magnetic Materials*, 385(0):282–285, 2015.


[168] K. Mbela, T. Moyo, and S.E Nadir Osman. Effects of annealing on exchange bias in $\text{Mg}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$ compounds prepared via the hydrothermal route. *Submitted*.

[169] K. Mbela, T. Moyo, M. Öztürk, and N. Akdoğan. Magnetic studies of $\text{Mn}_{0.2}\text{Fe}_x\text{Cr}_{1.8-x}\text{O}_3$ compounds prepared via the hydrothermal route. *Submitted*.